

Higgsless Electroweak Symmetry Breaking

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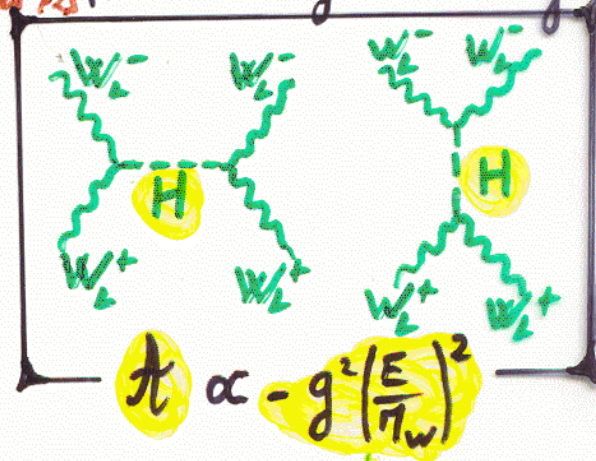
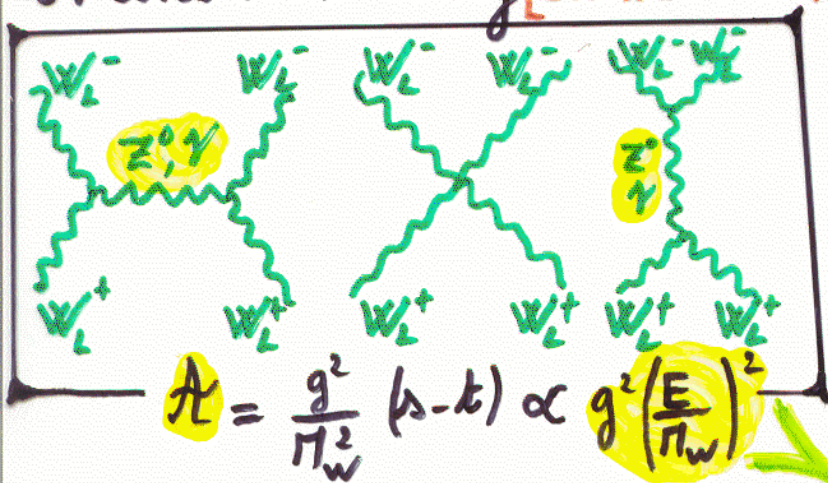
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Why do we need a Higgs?

1 To give mass to W & Z :

Spontaneously Broken Gauge Theory

UV consistent theory [Cornwall et al '73] [t Hooft] [Veltman '73] Renormalizable theory



Finite Amplitude

$$\mathcal{A} \propto g^2 \left(\frac{\pi_H}{\pi_w} \right)^2$$

($\Rightarrow m_H < 1 \text{ TeV}$)

2 To give mass to Quarks & Leptons

Chiral Theory: t_L & t_R have different couplings to W, Z

$$m_{t_L t_R}$$



$$m \frac{H}{v} t_L t_R$$

$$SU(2)_L \times U(1)_Y$$



$$SU(2)_L \times U(1)_Y$$



Higgs = a so useful particle ... yet unseen. A life without it?

Standard Scenario of EWSB

Weakly Coupled:

- $(\overline{15})5H$
- Little Higgs i.e. Higgs as a pseudo Goldstone boson

Strongly Coupled:

- (extended, walking, top color assisted) technicolor

Since the blooming of extradimensions,
two new approaches.

- Higgs = component of gauge field in extra dimension
- Symmetry breaking by boundary conditions
a.k.a.

Higgsless

$$m^2 = E^2 - \vec{p}_3^2 - \vec{p}_\perp^2$$

no need for a mass from a Higgs!

Symmetry Breaking From Boundary Conditions

Sym. Breaking Different BC's for
Different Gauge Directions

SU(2) \rightarrow U(1)

BCs

$$0 \quad \square_\mu A_\mu^a - \partial_\mu^2 A_\mu^a = 0 \quad \pi R$$

$$A_\mu^{1,2}|_0 = 0$$

$$\partial_\perp A_\mu^3|_0 = 0$$

$$\partial_\perp A_\mu^{1,2,3} = 0$$

$$m_\gamma(\omega) = 0$$

$$m_\gamma(k) = \frac{k}{R}$$

$$m_W(k) = \frac{2k+1}{2R}$$

$$A_\mu^1(x, y) = \sum_{k=0}^{\infty} \frac{1}{\sqrt{\pi R}} \sin \frac{(2k+1)y}{2R}$$

$$(W_\mu^{+(k)}(x) + W_\mu^{-(k)}(x))$$

$$A_\mu^2(x, y) = \sum_{k=0}^{\infty} \frac{i}{\sqrt{\pi R}} \sin \frac{(2k+1)y}{2R}$$

$$(W_\mu^{+(k)}(x) - W_\mu^{-(k)}(x))$$

$$A_\mu^3(x, y) = \sum_{k=0}^{\infty} \sqrt{\frac{2}{2^k k! \pi R}} \cos \frac{ky}{R}$$

$$Z_\mu^{(k)}(x)$$

What are the most general BC's?

What is the nature of the Breaking?

Can we get a realistic EWSB model?

Here: $\gamma: m=0$; $W: m=\frac{1}{2R}$; $Z \equiv \gamma^{(1)}: m=2m_W$

BC's for 5D Scalar Theory

$$S = \int d^4x \int_0^{\pi R} dy \left(\frac{1}{2} \partial_\mu \phi \partial^\mu \phi - V(\phi) \right) + \int_{y=0, \pi R} d^4x \frac{1}{2} \Pi_{0, \pi R}^2 \phi^2$$

integration by part

Boundary Term

$$\delta S = \int_{y=0, \pi R} d^4x \delta \phi (\partial_y \phi + \Pi_{0, \pi R}^2 \phi) + \text{Bulk Part}$$

BC's
Bulk Eq. of motion

$$\delta \phi (\partial_y \phi + \Pi_{0, \pi R}^2 \phi) = 0 \qquad \square_5 \phi = -V'(\phi)$$

Consistent BC's :

(i) Dirichlet

$$\phi_{0, \pi R} = \text{cst.}$$

(ii) Mixed BC's

$$\partial_y \phi = -\Pi^2 \phi$$

$\pi \rightarrow \pi R$ → Dirichlet
 $\pi \rightarrow 0$ → Neumann

(iii) Non trivial cancellation among various boundary terms

BC's for 5D Gauge Theory

$$S = \int d^4x \int_0^{\pi R} dy \left(-\frac{1}{4} F_{\mu N}^a F^{a \mu N} - \frac{1}{2\xi} (\partial_\mu A^{a\mu} - \xi \partial_5 A_5^a)^2 \right)$$

Gauge Fixing Terms

$$\delta S = \int_{y=0, \pi R} d^4x \left(\frac{1}{2} F_{\mu 5}^a \delta A^{a\mu} + (\partial_\mu A^{a\mu} + \xi \partial_5 A_5^a) \delta A_5^a \right) + \text{Bulk Part}$$

Consistent BC's:

(i) $A_\mu^a = 0$, $A_5^a = \text{const.}$

(ii) $A_\mu^a = 0$, $\partial_5 A_5^a = 0$

(iii) $\partial_5 A_\mu^a = 0$, $A_5^a = \text{const.}$

(iv) non trivial cancellation among various boundary terms.

Gauge Symmetry Breaking

different BC's for different gauge directions

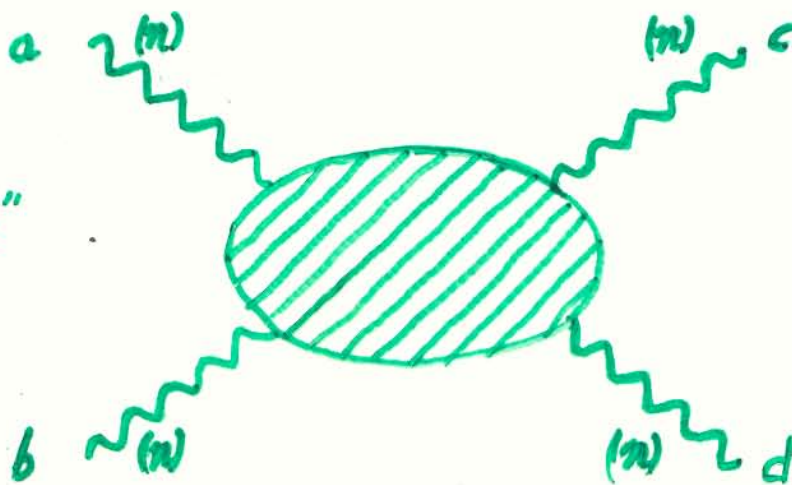
(No automorphism restriction; No Parity restriction)

No Explicit Symmetry Breaking Terms

Soft Breaking?

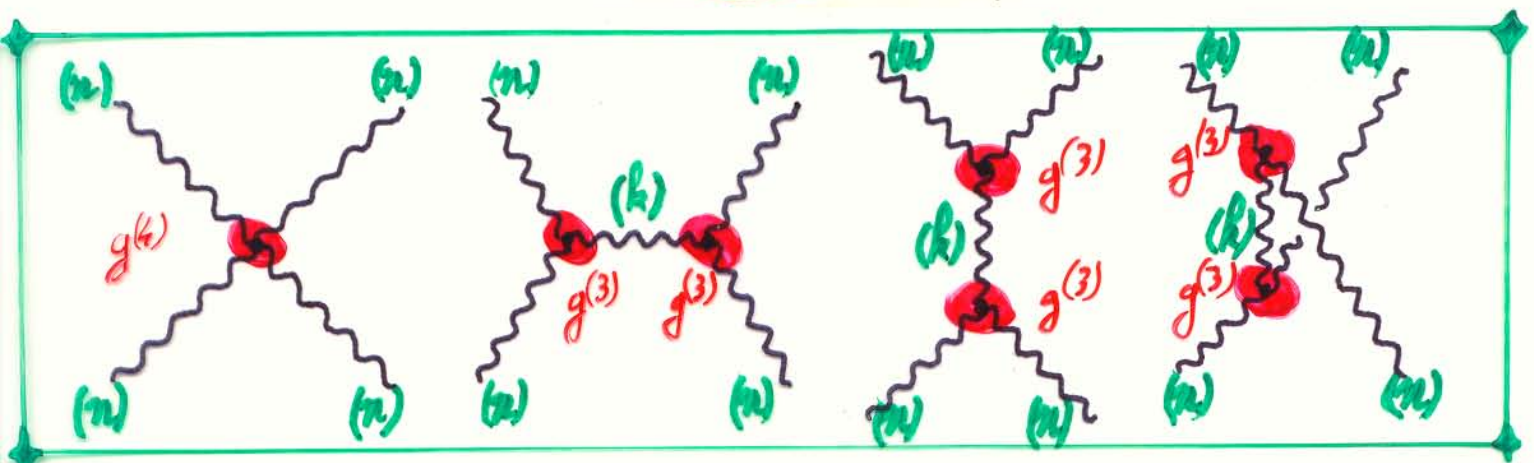
(Elastic) Scattering Amplitude

Same KK
"in" and "out"
...



(longitudinal polarization
 $\epsilon_\mu = \left(\frac{|\vec{p}|}{\pi}, \frac{E}{\pi} \frac{\vec{p}}{|\vec{p}|} \right)$)

$$A = A^{(4)} \left(\frac{E}{\pi_n} \right)^4 + A^{(2)} \left(\frac{E}{\pi_n} \right)^2 + A^{(0)} + \dots$$



$$A^{(4)} = i \left(g_{nnnn}^2 - \sum_k g_{nnk}^2 \right) \left(\int^{abe} \int^{cde} (3 + 6c_\theta - c_\theta^2) + 2(3 - c_\theta^2) \int^{ace} \int^{bde} \right)$$

$$A^{(2)} = i \left(4g_{nnnn}^2 - 3 \sum_k g_{nnk}^2 \frac{\pi k^2}{\pi_n^2} \right) \left(\int^{ace} \int^{bde} - \sin^2 \frac{\theta}{2} \int^{abe} \int^{cde} \right)$$

K, K₁ Theory

$$A_\mu^a = \sum_k \int_{(m)}^a \epsilon_\mu e^{i p_n \cdot x}$$

$$(p_n^2 = m_n^2)$$

Wave functions:

Bulk Eq. : $f_n'' + m_n^2 f_n = 0$

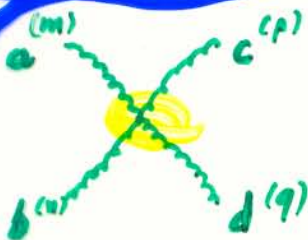
BC's Eq. : $f_n' = \nu f_n |_{0, \pi R}$

⇒ Spectrum & Wave functions

Effective Couplings:



$g_{\text{cubic}} \rightarrow g_{mnp}^{abc} = \int_0^{\pi R} dy f_m^a(y) f_n^b(y) f_p^c(y) g_5$



$g_{\text{quartic}}^2 \rightarrow g_{mnpq}^{abcd} = \int_0^{\pi R} dy f_m^a f_n^b f_p^c f_q^d g_5^2$

(unless flat wavefunction, $g_{\text{quartic}}^2 \neq g_{\text{cubic}}^2$)
 deviations in the W, Z couplings
 observable @ NLC ?

Sum Rules

or unitarity without a Higgs!

E^4 terms

$$g_{nnnn}^2 - \sum_k g_{nnk}^2$$

$$= g_5^2 \int_0^{\pi R} dy \int_0^{\pi R} dz \, f_n^2(y) f_n^2(z) \underbrace{\sum_k f_k(y) f_k(z)}_{\delta(y-z)}$$

$$= 0 \quad [\text{Csáki, C.G., Murayama, Pilo, Terning '03}]$$

Completeness of KK modes
since ∂_5^2 is selfadjoint

E^2 terms

$$4 g_{nnnn}^2 \Pi_n^2 - 3 \sum_k g_{nnk}^2 \Pi_k^2$$

$$\sum_k \Pi_k^2 \int_0^{\pi R} dy \int_0^{\pi R} dz \, f_n^2(y) f_n^2(z) f_k(y) f_k(z) = \frac{4}{3} \Pi_n^2 \int_0^{\pi R} dy \, f_n^4(y)$$

integration by part
 $f_k'' = -\Pi_k^2 f_k$

up to boundary terms ...

$$-\frac{2}{3} [f_n^3 f_n']_0^{\pi R} + 2 \sum_k [f_n f_n' f_k]_0^{\pi R} \int_0^{\pi R} dy \, f_n^2 f_k$$

$$- \sum_k [\Pi_n^2 f_k']_0^{\pi R} \int_0^{\pi R} dy \, f_n^2(y) f_k(y)$$

that cancel for **Dirichlet** and **Neumann BC's**.

For **mixed BC's**: exchange of KK's doesn't unitarize \mathcal{A}
 \hookrightarrow needs for more degrees of freedom
 (Higgs localized on the brane)

Spontaneous Breaking by BC's

A counter example to Cornwall et al. theorem?

No!

E^2 cancellation requires an infinite # KK's

$$g_{nnnn}^{(E)} = \sum_k g_{nnkk}^{(E)} = \sum_k g_{nnkk}^{(E)} \frac{3\pi R^2}{4\pi n^2}$$

With a finite # KK's:

(an effective theory of massive W, Z above Π_w)

E ↑ New Physics
(Higgs / Strong coupling)

True Cutoff (5D)

not directly set by the weak scale ...
(too high to be observed)

Weakly coupled states observable at low energy

$$\left(\frac{24\pi^3}{g_5^2} = \frac{12\pi^2 \Pi_w}{g_4^2} \right)$$

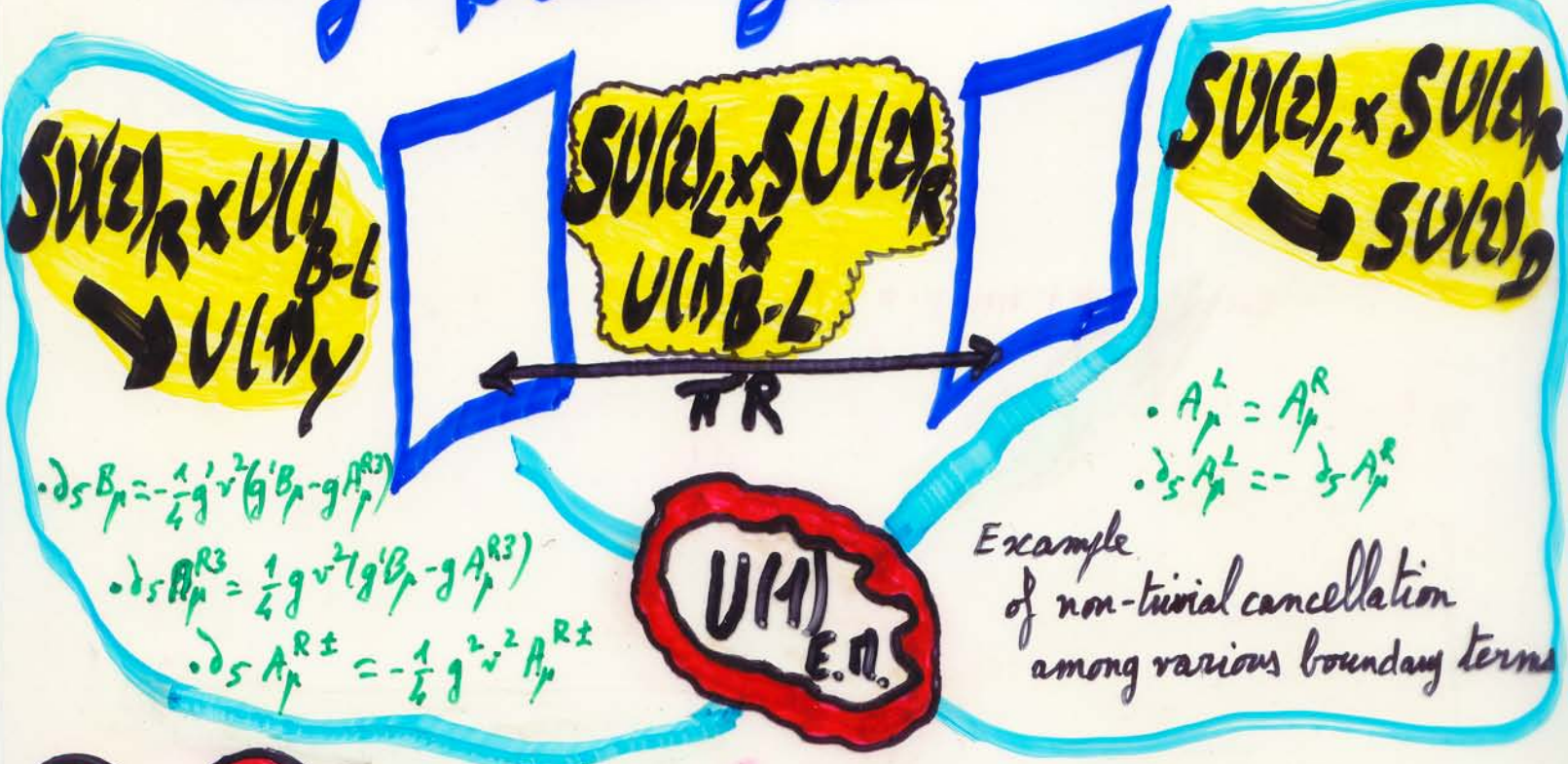
(even in flat space, already a factor 10)

Naive Cutoff

Weak scale

No need for a scalar field at low energy anymore ...

Toy Model of EW/SB



Spectrum



$m \tan 2m\pi R = \frac{1}{4} g_s^2 v^2$
 $m \approx \frac{2k+1}{4R} + \mathcal{O}(1/R^2 v)$

BRANE Higgs DECOUPLING

$m \tan m\pi R = \frac{g_s^2 + 2g_s'^2 v^2}{8} - \frac{g_s'^2 v^2}{8} \tan^2 m\pi R$
 $m = \frac{k}{R} \pm \frac{1}{\pi R} \arctan \sqrt{\frac{2g_s'^2 + g_s'^2}{g_s^2}} + \mathcal{O}(1/R^2 v)$

Coupling to matter @ $y=0$

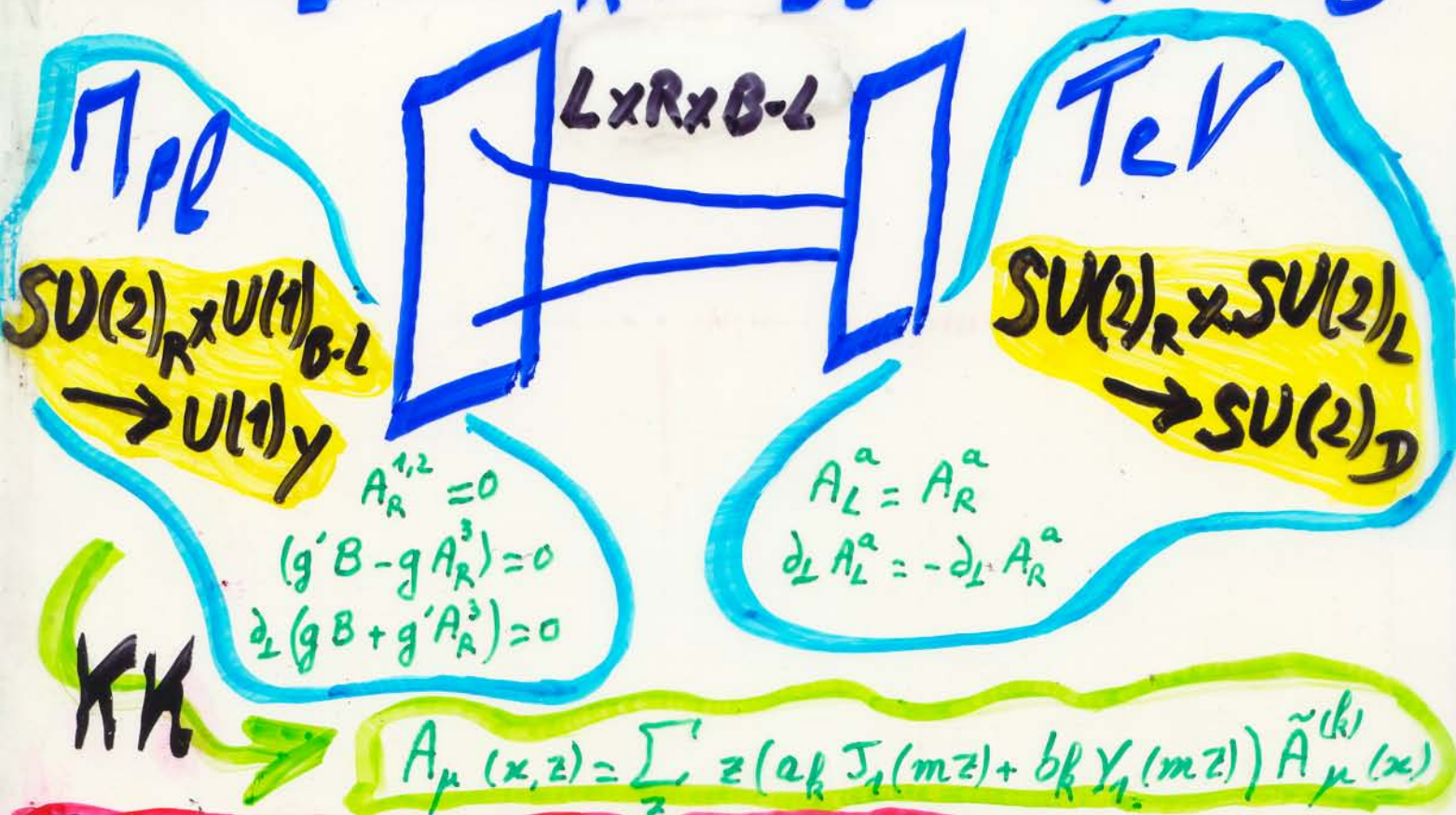
usual couplings to γ, W^\pm, Z BUT

$\rho = \frac{\Pi_W^2}{\Pi_Z^2 \cos^2 \theta_W} \sim 1.90$

... and too light w', z'

[Csáki, Gajjaran, Murayama, Pilo, Terning '03]

$SU(2)_L \times SU(2)_R \times U(1)_{B-L}$ in AdS₅



W

$$(R_0 - R'_0)(R_1 - R'_1) + (R'_1 - R_0)(R'_0 - R_1) = 0$$

$$m_W^2 = \left(R_{TeV}^2 \ln \frac{R_{TeV}}{R_{IR}} \right)^{-1}$$

$$R_i, R'_i = \frac{Y_i(mz)}{J_i(mz)} |_{\Pi_{PR}, TeV}$$

Z

$$g^2 (R_0 - R'_0)(R_1 - R'_1) + (R'_1 - R_0)(R'_0 - R_1) = 2g'^2 (R_0 - R'_1)(R'_0 - R_1)$$

$$m_Z^2 = \frac{g^2 + 2g'^2}{g^2 + g'^2} \left(R_{TeV}^2 \ln \frac{R_{TeV}}{R_{IR}} \right)^{-1}$$

Solution of Little Hierarchy pb.!

KK's : $(SU(2)_R \text{ multiplet})$
 ... because of TeV localization ...

$$m_W^{(2)} \sim m_Z^{(4)} \sim m_\gamma^{(2)} \sim 1.2 \text{ TeV}$$

$$m_W^{(3)} \sim m_Z^{(3)} \sim 1.9 \text{ TeV}$$

AdS

EFT dual

[Csáki, C.C., Pilo, Terning '03
 Agashe, Delgado, Flay, Sundrum '03]

Walking Technicolor!

EW Effective Lagrangian

Gauge Sector

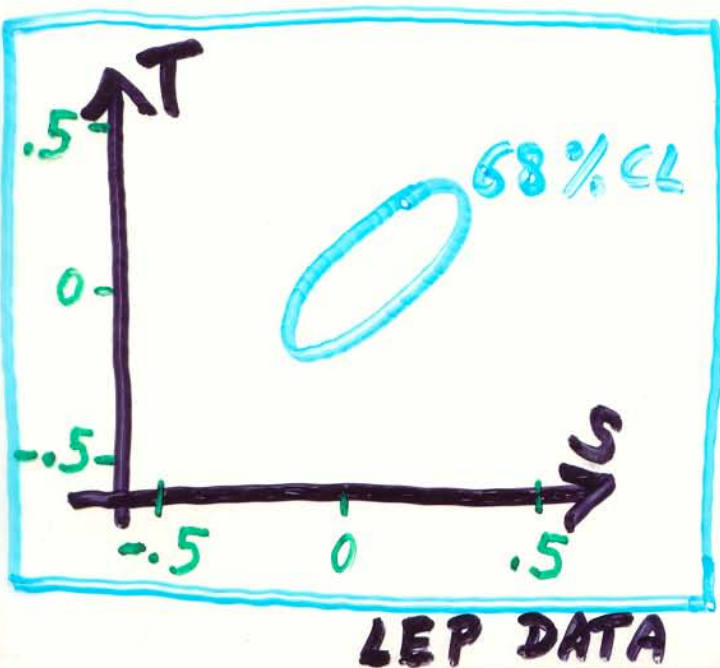
$$-\frac{1}{2} W_{\mu\nu}^- W^{+\mu\nu} + \Pi_W W_{\mu}^+ W^{-\mu} - \frac{1}{4} Z_{\mu\nu} Z^{\mu\nu} + \frac{1}{2} \Pi_Z Z_{\mu} Z^{\mu} - \frac{1}{4} \gamma_{\mu\nu} \gamma^{\mu\nu}$$

Gauge Fermion Interactions:

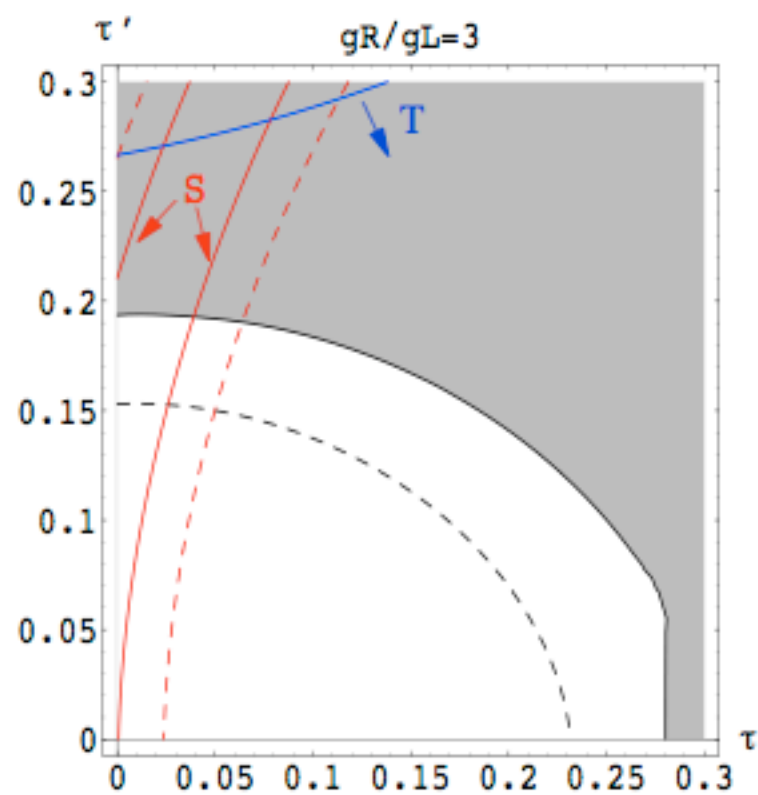
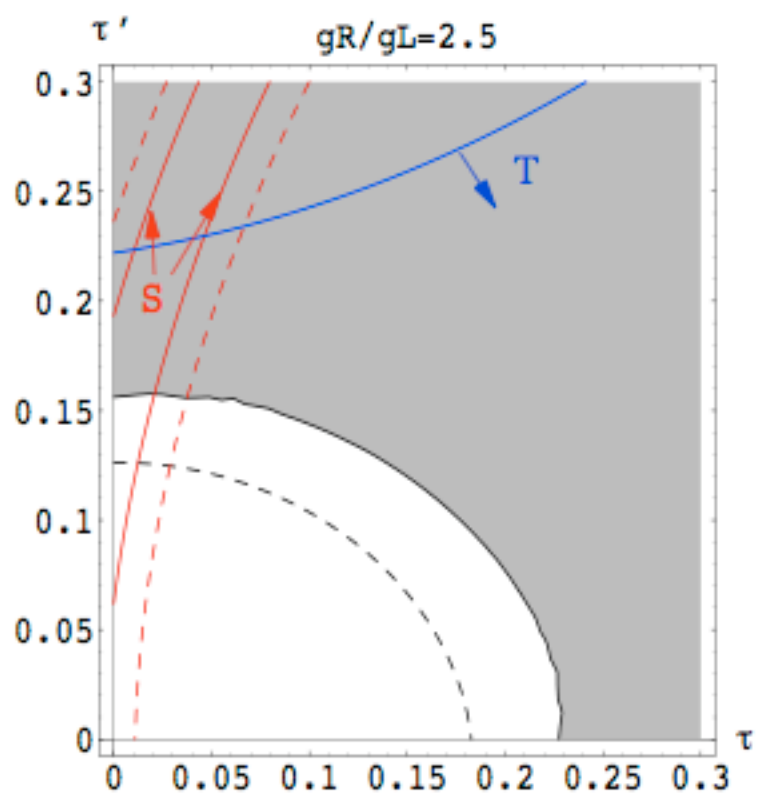
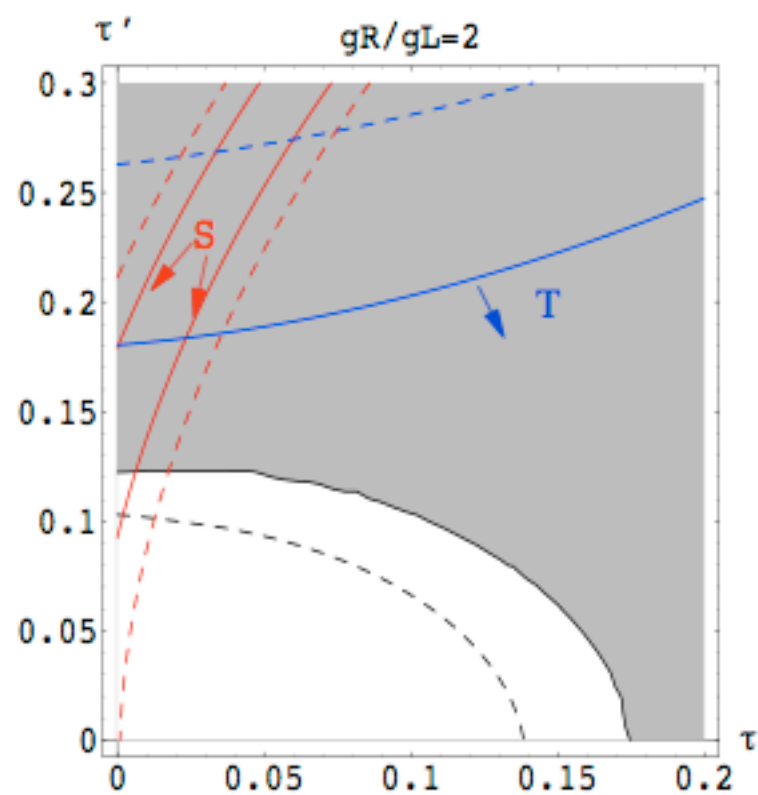
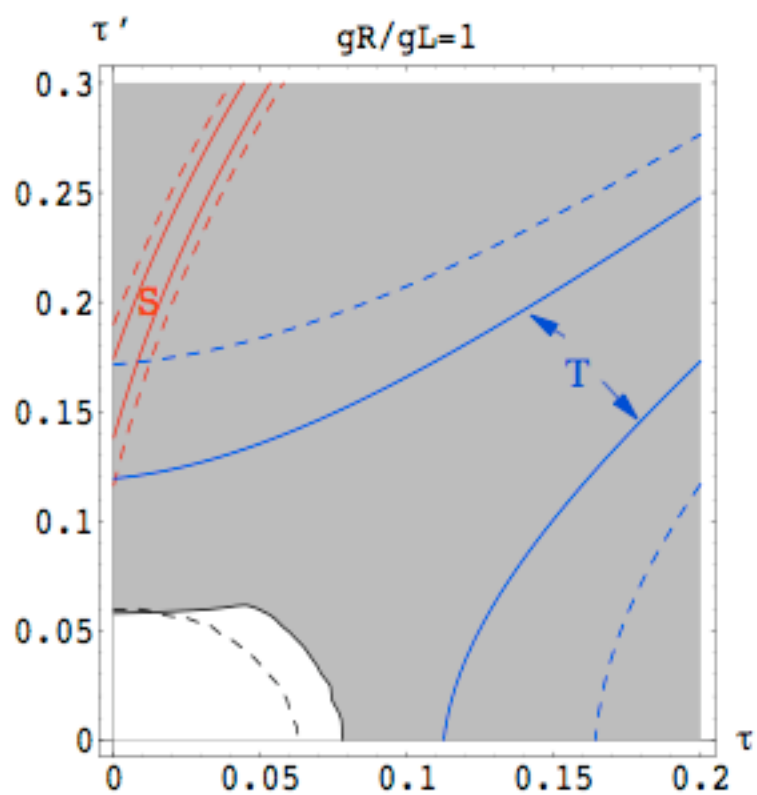
$$\left(-ig W_{\mu}^{\pm} T^{\pm} - ig' \sin \theta_W (T_{3L} - \tan \theta_W \frac{Y}{2}) Z_{\mu} - ie \gamma_{\mu} \right) \psi$$

Tree Level + Quadratic order

6 parameters: $\begin{cases} g_{SU(2)_L} & g'_{U(1)_Y} & v & (\Pi_Z) \\ S & T & U & \end{cases}$
(measure the deviations to s.m.)

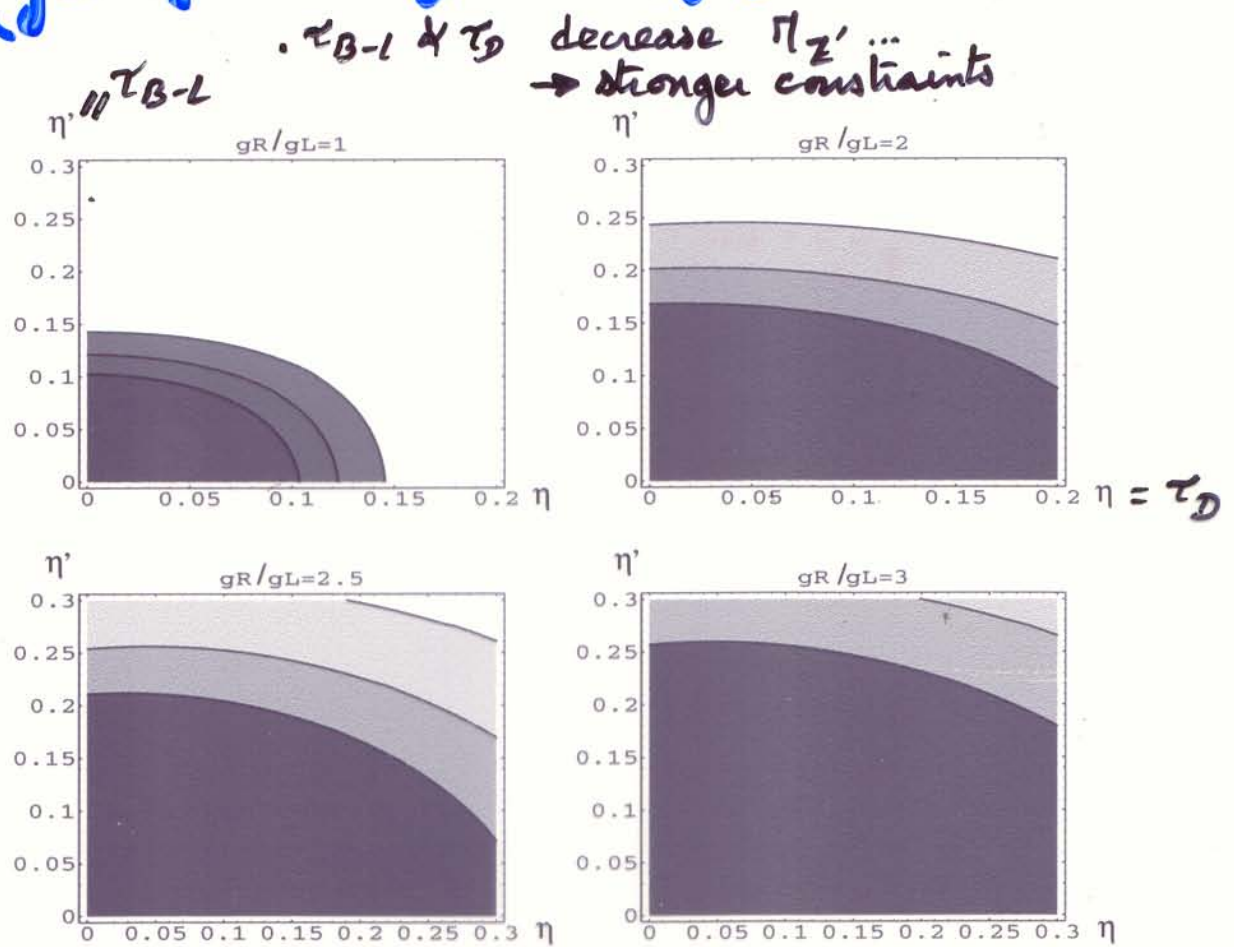


SM tested
experimentally
at 0.1%



LEP constraints on Z'

(fit of $SU(2)_C \times U(1)_B$ 8-1 TeV R.t.)



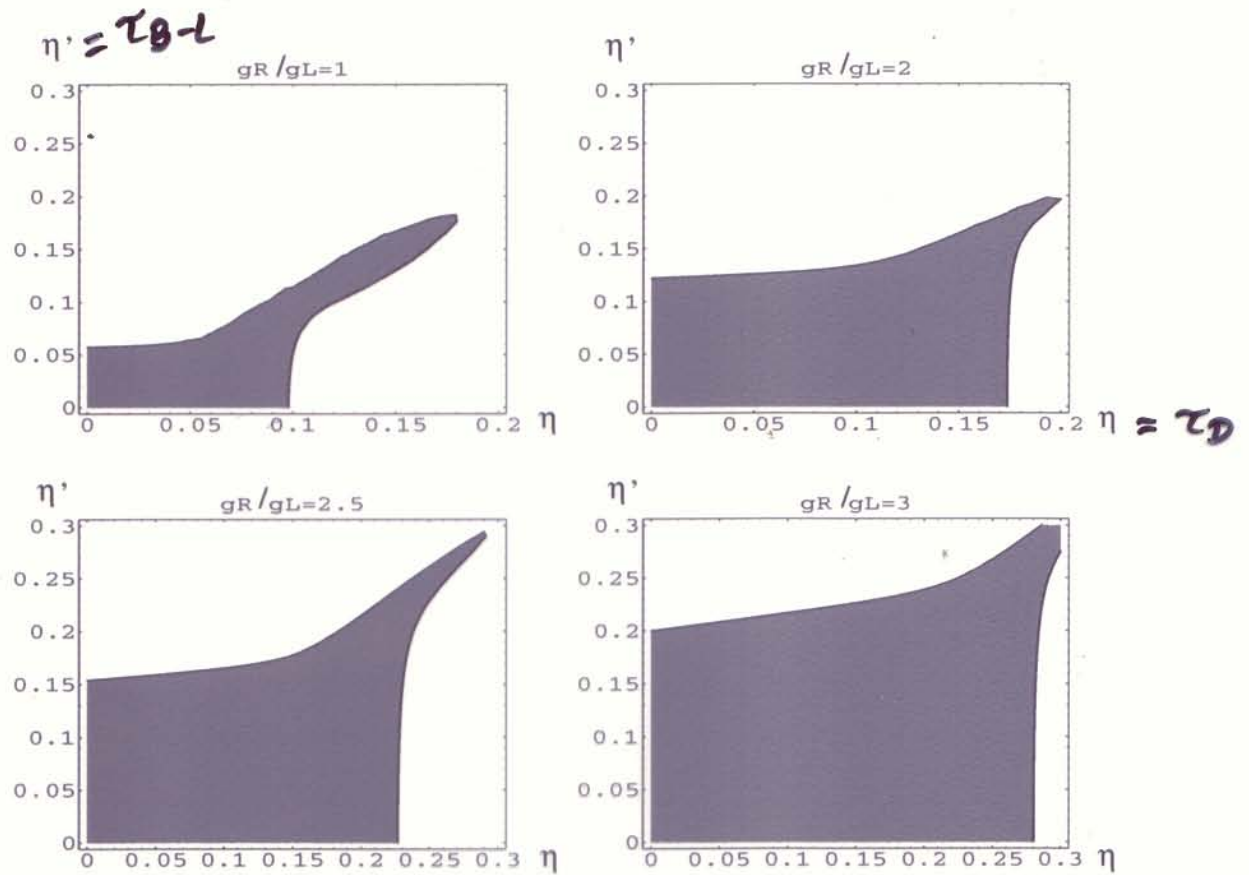
Contours: 5%, 7%, 10%



light Z'
 $\rightarrow \delta\sigma(e^+e^- \rightarrow \mu^+\mu^-)$

search for deviation for the cross section of $e^+e^- \rightarrow \mu^+\mu^-$
 due to the light Z' from the S.M. prediction @ 200 GeV.
 (deviation < 3-5%)

Tevatron Constraints on Z' (Run I @ 110 pb⁻¹)



Search for dilepton pairs with large transverse momentum.
(bound on production cross section \times branching fraction)

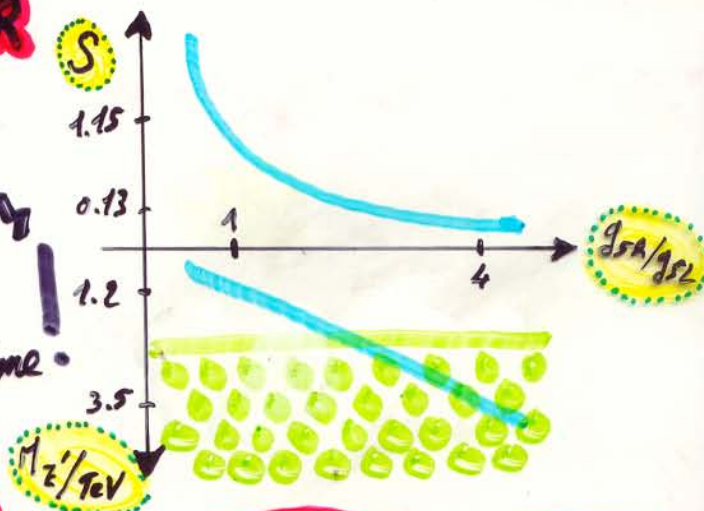
How to Suppress S

[Cacciapaglia, Csáki, C.G. TERNING
HEP-PH/0401160]

Asymmetric $SU(2)_L \times SU(2)_R$

$$S = S_0 \cdot \frac{2}{1 + (g_{SR}/g_{SL})^2}$$

EW Precision Test
v.s.
Weakly Coupled Regime



Brane localized kinetic terms

$SU(2)_L$

$U(1)_Y$

PL

$$\cdot -\frac{1}{2} \tilde{\kappa}_L W_{\mu\nu}^{(L)} W_{\mu\nu}^{(L)}$$

$$\cdot -\frac{1}{4} \tilde{\kappa}_Y Y_{\mu\nu} Y^{\mu\nu}$$

$SU(2)_R$

$U(1)_{B-L}$

TeV

$$\cdot -\frac{1}{2} \tilde{\kappa}_D W_{\mu\nu}^{(D)} W_{\mu\nu}^{(D)}$$

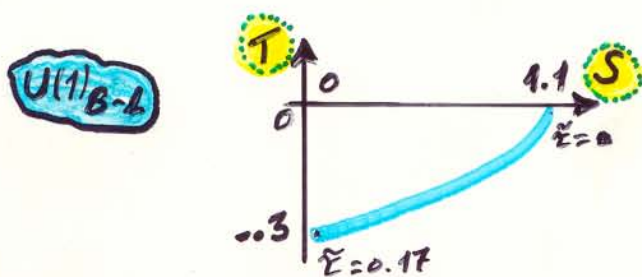
$$\cdot -\frac{1}{4} \tilde{\kappa}_{B-L} B_{\mu\nu} B^{\mu\nu}$$

$(\tilde{\kappa}_i = \kappa_i / R \log(R'/R))$

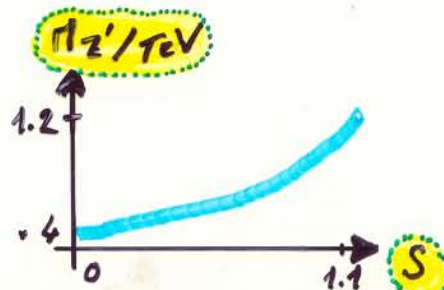
$$S = S_0 \cdot \frac{2}{1 + (g_{SR}/g_{SL})^2} \cdot \frac{1}{1 + \tilde{\kappa}_L} + \frac{8\pi}{g_L^2} \cdot \frac{2}{1 + (g_{SR}/g_{SL})^2} \cdot \frac{\tilde{\kappa}_D}{1 + \tilde{\kappa}_L} - \frac{16\pi}{g_L^2} \cdot \frac{g_{SR}}{g_{SL}^2 + g_{SR}^2} \cdot \frac{1}{1 + \frac{(g_{SR})^2}{(g_{SL})^2}} \cdot \tilde{\kappa}_{B-L}$$

$SU(2)_L$, $SU(2)_D$, $U(1)_Y$

- loss of perturbative unitarity
- tachyonic KK's ($-m^2 \sim \text{TeV}^2$)

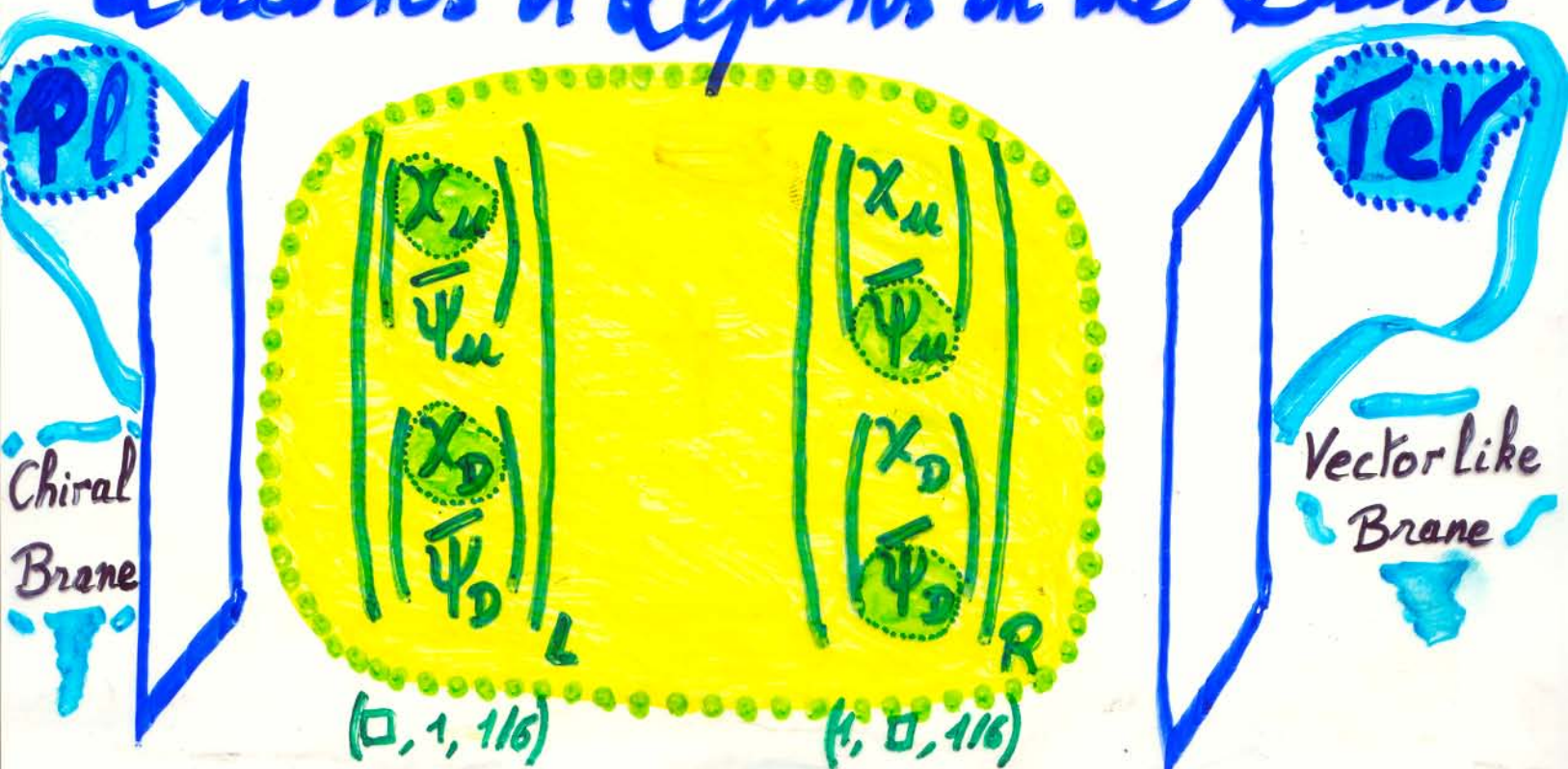


Direct Detection
OK



Precision Measurements
Non oblique corrections

Quarks & Leptons in the Bulk



Bulk
L x R x B-L

PL
L x Y

TeV
D x B-L

4D
Q

$\begin{pmatrix} X_u \\ X_d \end{pmatrix}_L$	$(\square, 1, 1/6)$	$\square, 1/6$	$(\square, 1/6)$	$\begin{matrix} 2/3 \\ -1/3 \end{matrix}$
$\begin{pmatrix} \Psi_u \\ \Psi_d \end{pmatrix}_L$	$(\bar{\square}, 1, -1/6)$	$(\bar{\square}, -1/6)$	$(\bar{\square}, -1/6)$	$\begin{matrix} -2/3 \\ 1/3 \end{matrix}$
$\begin{pmatrix} X_u \\ X_d \end{pmatrix}_R$	$(1, \square, 1/6)$	$\begin{matrix} (1, 2/3) \\ (1, -1/3) \end{matrix}$	$(\square, 1/6)$	$\begin{matrix} 2/3 \\ -1/3 \end{matrix}$
$\begin{pmatrix} \Psi_u \\ \Psi_d \end{pmatrix}_R$	$(1, \bar{\square}, -1/6)$	$\begin{matrix} (1, -2/3) \\ (1, 1/3) \end{matrix}$	$(\bar{\square}, -1/6)$	$\begin{matrix} -2/3 \\ 1/3 \end{matrix}$

$$Q = Y + T_3 L$$

$$Y = B - L + T_3 R$$

Chiral & Massless 4D Fermion

(from a 5D vectorlike & massive fermion...)



$$S = \int d^5x \left(\frac{R}{2}\right)^4 \left(-i \bar{\chi} \bar{\sigma}^\mu \partial_\mu \chi - i \bar{\psi} \sigma^\mu \partial_\mu \psi + \frac{1}{2} (\psi \overleftrightarrow{\partial}_5 \chi - \bar{\chi} \overleftrightarrow{\partial}_5 \bar{\psi}) + \frac{c}{2} (\psi \chi + \bar{\chi} \bar{\psi}) \right)$$

$$\delta S_{10} = \frac{1}{2} \int d^4x \left(\frac{R}{2}\right)^4 (\delta \chi \psi - \delta \psi \chi + \text{f.c.})$$

Bulk Eqs of Motion & Boundary Conditions

$$\left. \begin{aligned} -i \bar{\sigma}^\mu \partial_\mu \chi - \partial_5 \bar{\psi} + \frac{c+2}{2} \bar{\psi} &= 0 \\ -i \sigma^\mu \partial_\mu \bar{\psi} + \partial_5 \chi + \frac{c-2}{2} \chi &= 0 \end{aligned} \right\}$$

the bulk eqs. of motion restrict the BCs.

$$\chi_1 = 0 \Rightarrow \partial_5 \psi_1 = \frac{c+2}{2} \psi_1$$

no independent BCs for χ and ψ !

χ Dirichlet $\leftrightarrow \psi$ Neumann
 ψ Dirichlet $\leftrightarrow \chi$ Neumann

Chiral Spectrum

Zero Mode

$$\frac{c}{2} (\psi \chi + \text{f.c.})$$



5D mass \Rightarrow localization of the zero mode

$$\chi = \left(\frac{z}{R}\right)^{2-c} \frac{1}{R^c} \sqrt{\frac{R-2c}{R^{4-2c} - R^{4-2c}}} \psi = 0$$

$c > 1/2$ remains normalizable even if $R' \rightarrow \infty$
 Planck Brane localized
 $c < 1/2$ remains normalizable even if $R \rightarrow 0$
 TeV Brane localized

Delocalized Fermion to Suppress S

gauge boson/fermion coupling = overlap of wavefunctions

$$\left(T_{3L} + \underbrace{\frac{g_{SB} \int_R^{R'} dz \left(\frac{R}{z}\right)^4 \int_{\chi_2}^2 \int_{B-L} Y}{g_{SL} \int_R^{R'} dz \left(\frac{R}{z}\right)^4 \int_{\chi_2}^2 \int_{L3}}}_{-g'/g} \right) Z_\mu \chi_L$$

gauge coupling matching
W and Z normalizations depend on the fermion profile

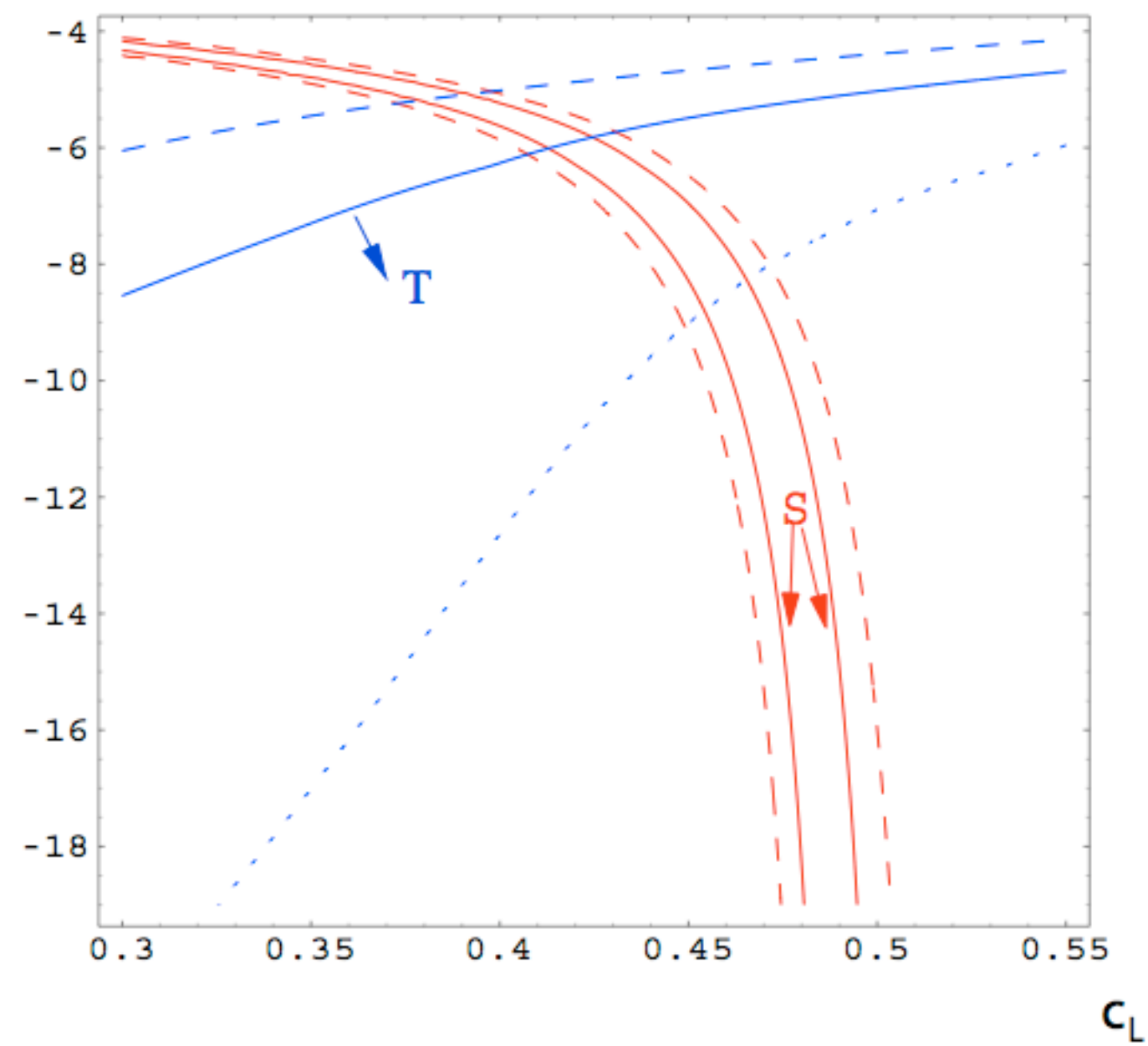
$$\int_{\chi_L}^{(z)} = \frac{1}{R'} \sqrt{\frac{1-2c}{R'^{4-2c} - R^{4-2c}}} \left(\frac{z}{R}\right)^{2-c} \cdot \begin{matrix} c \gg 1/2 & \text{Pl localized} \\ c \ll -1/2 & \text{TeV localized} \end{matrix}$$

Pl fermion \rightarrow positive contribution to S } somewhere in middle
TeV fermion \rightarrow negative contribution to S } $S \sim 0$

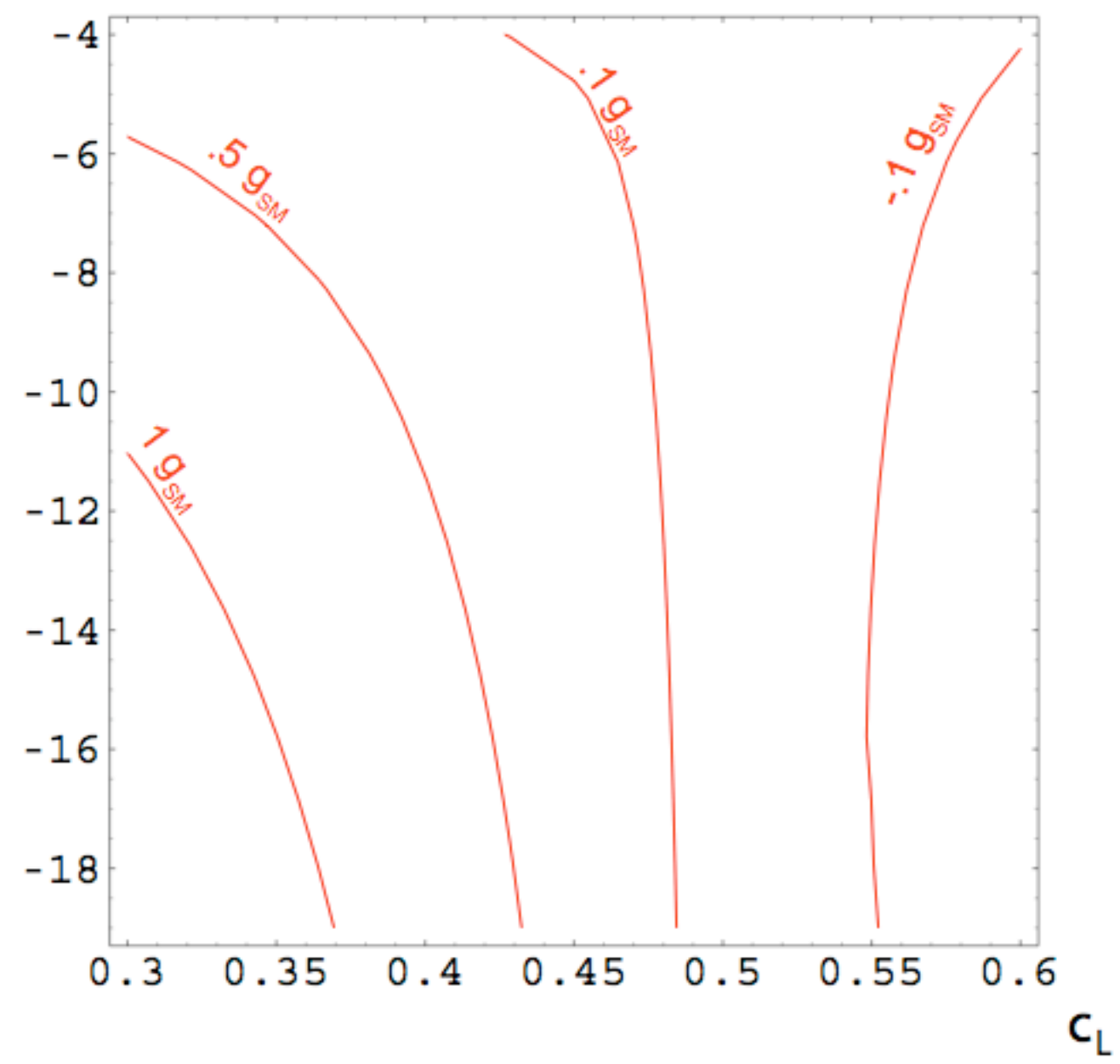
Allow to suppress S without modifying Π_Z

(no trouble with LEP nor Teratron constraints)

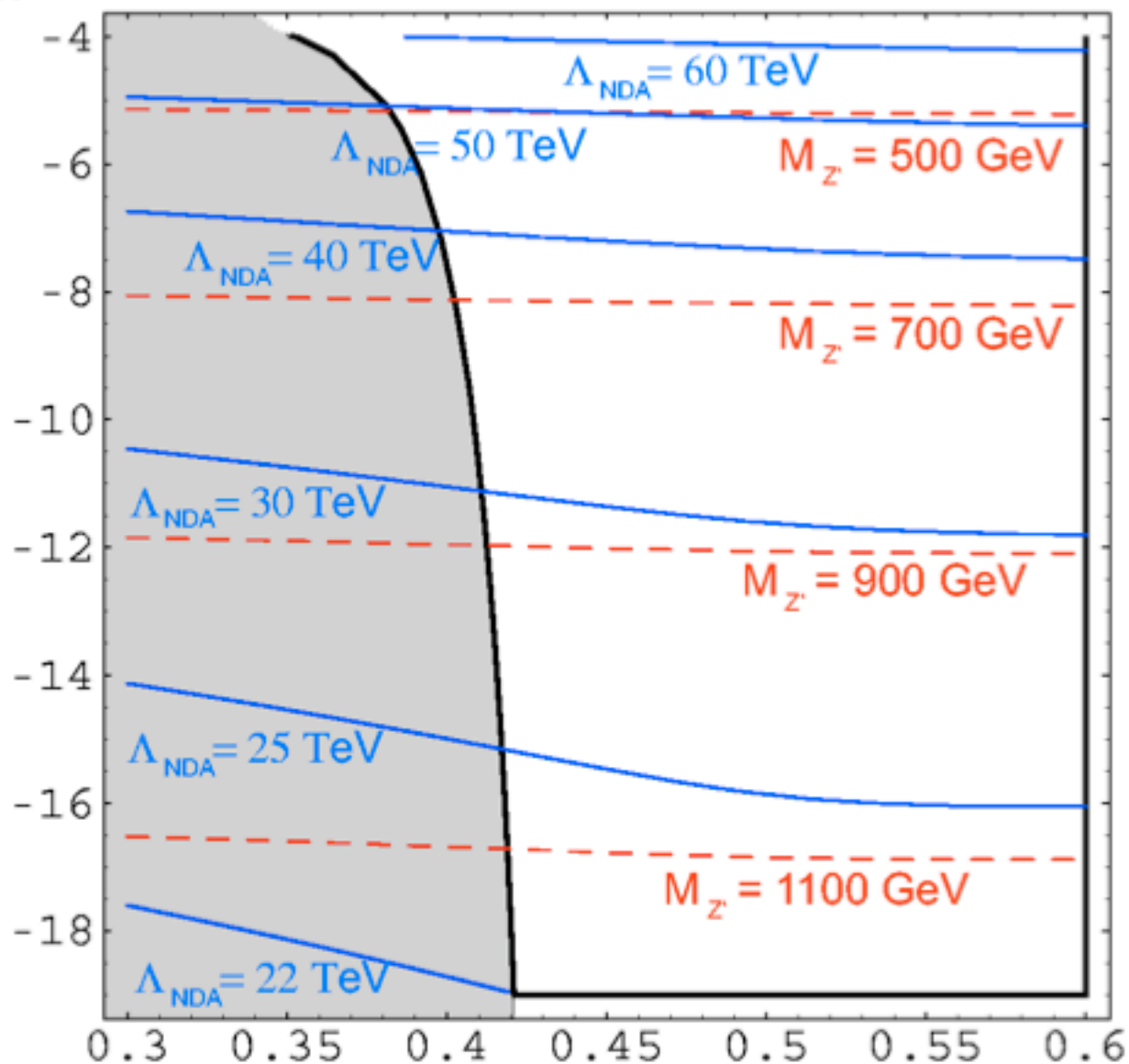
$\text{Log}_{10} R [\text{GeV}^{-1}]$



$\text{Log}_{10} R [\text{GeV}^{-1}]$



$\text{Log}_{10} R [\text{GeV}^{-1}]$



c_L

Gauge Coupling Non Universality

fermion mass \leftrightarrow wave fct profile in the bulk

coupling \leftrightarrow wave fct overlap

different masses \Rightarrow different couplings to W, Z

Non Universal Couplings

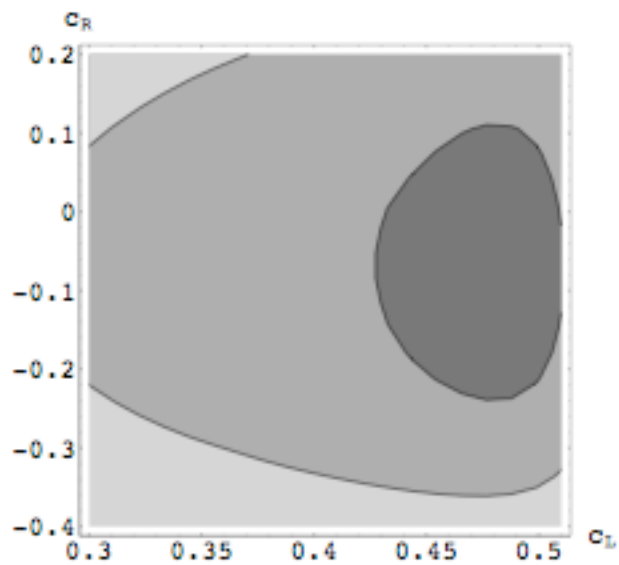
First two generations:

$$\frac{\delta g_{SM}}{g_{SM}} \sim \mathcal{O}\left(\frac{m}{\text{TeV}}\right) \approx 0.1\% \text{ at most}$$

Third generation:

$m_t \approx 178 \text{ GeV}$ important distortion of the profile

large $\delta g_{Z b_L \bar{b}_L}$ expected.



Collider Signals

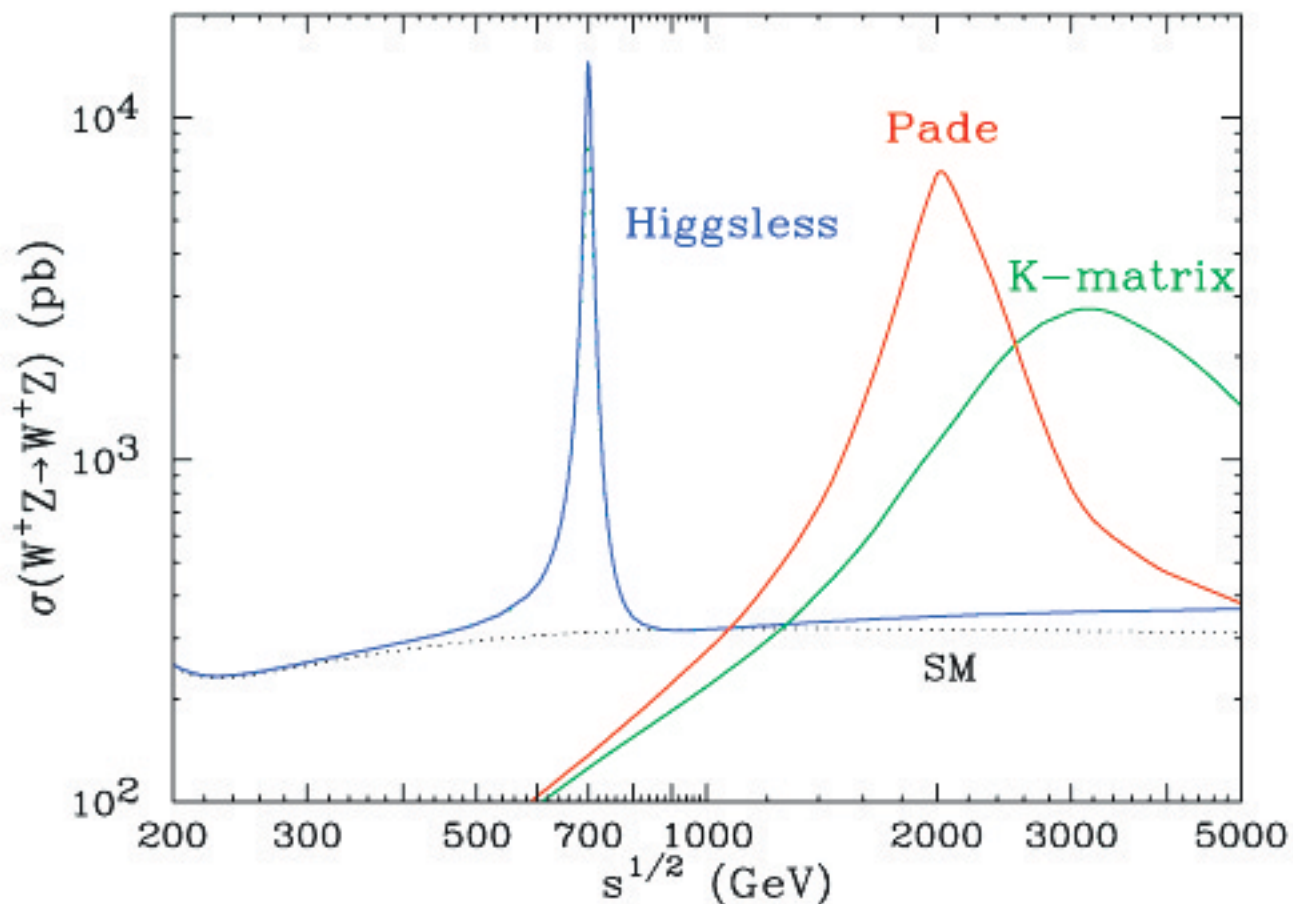
[Birkedal, Natchez, Perelstein]
'04

General Picture:

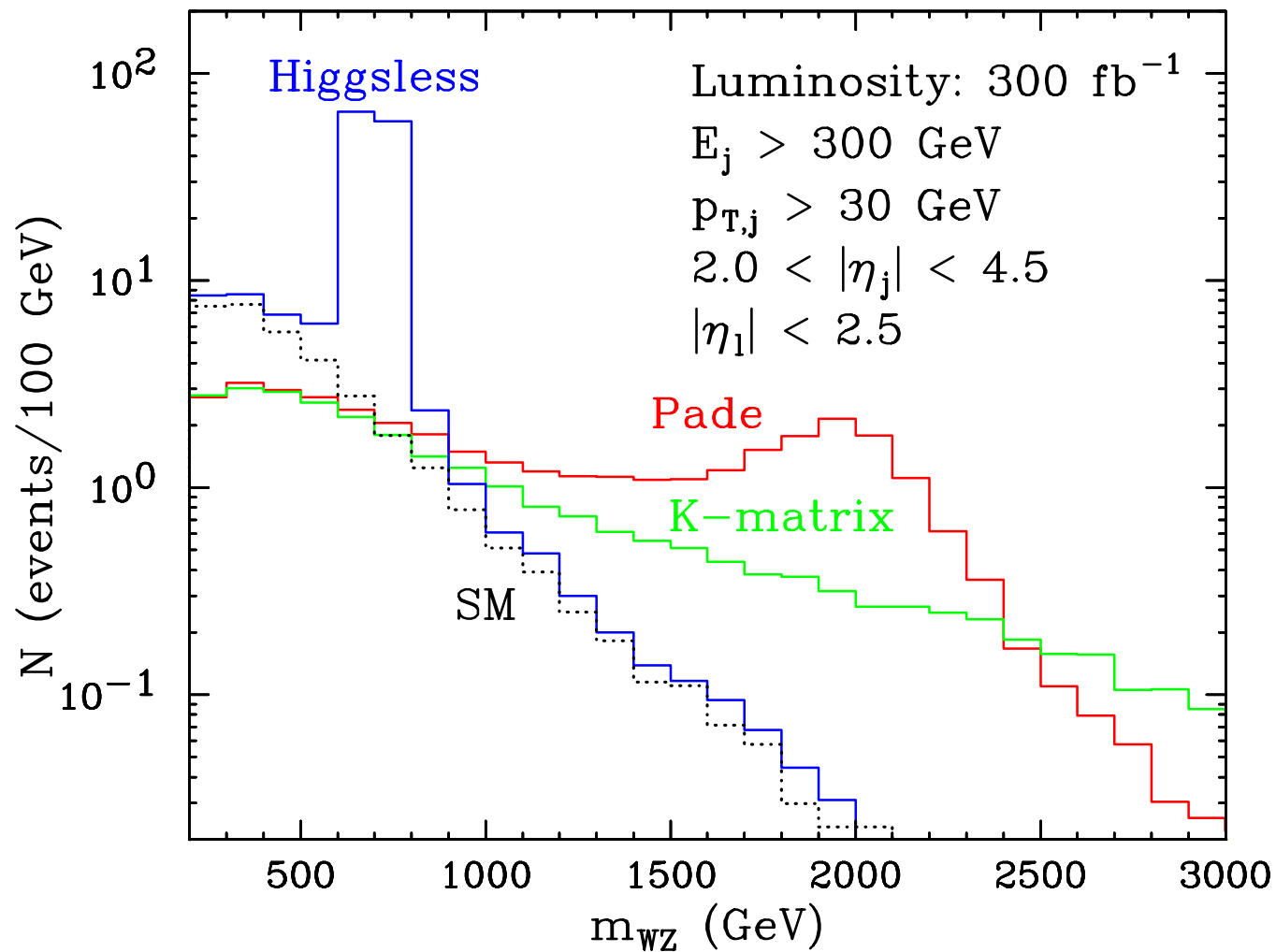
unitarity restored by vector resonances
whose masses and couplings are constrained by
the unitarity sum rules.

$$g_{WWZ} \lesssim \frac{g_{WWZ} \Pi_Z^2}{\sqrt{3} \Pi_{W'} \Pi_W}$$

$$\Gamma(W' \rightarrow WZ) \simeq \frac{\alpha \Pi_{W'}^3}{144 \Delta_W^2 \Pi_W^2}$$



WZ elastic scattering cross sections in the SM (dotted), the Higgsless model (blue) and two technicolor-like models



Conclusions

LHC will tell us
how EW symmetry
is broken!

We can see a Higgs.
But there is still room for
interesting/exciting
surprises ...
