

Theories of EW symmetry breaking and precision data after LEP2

- 1) The little hierarchy 'problem'
- 2) Relevance of LEP2
- 3) Universal models: \hat{S}, \hat{T}, W, Y
- 4) Extra d, little Higgs, SUSY, ...

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From works with Barbieri, Marandella, Pomarol, Rattazzi, Schappacher

...and its 'solutions'

A lot of activity before LHC... Two types of solutions:

I New symmetry implies $m_h = 0$; its breaking gives the EW scale

- **Supersymmetry:** $t \rightarrow \tilde{t}$ stop stops top.
- Attempts with scale symmetry, 5d gauge invariance, **little Higgs**.

II h becomes an extended object $1/\Lambda \sim \text{TeV}$

- **Technicolor:** $h = \text{hadron of a QCD-like group with } \Lambda_{\text{TC}} \lesssim \text{TeV}$
- **Large extra dimensions:** $h = \text{string with length } \gtrsim 1/\text{TeV}?$
- Warped extra dimension (AdS dual to CFT 'walking technicolor')

Precision data disfavour type II solutions

Extended particles \leftrightarrow form factors

LEP finds that SM fermions, gauge bosons and also the Higgs are point-like.

(Although the Higgs has not been discovered, its properties have been tested because the 3 massive SM vector bosons acquired a longitudinal polarization eating 3 components of the Higgs doublet).

Form-factors in QFT are introduced as higher dimensional operators, that encode the low energy effects of new physics too heavy to be directly seen.

Even restricting to $SU(2)_L \otimes U(1)_Y$, B, L, B_i, L_i , CP symmetric operators...

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{SM}} + \mathcal{O}/\Lambda^2$$

| operator \mathcal{O} | affects | constraint on Λ |
|---|-----------------------------|-------------------------|
| $\frac{1}{2}(\bar{L}\gamma_\mu\tau^a L)^2$ | μ -decay | 10 TeV |
| $\frac{1}{2}(\bar{L}\gamma_\mu L)^2$ | LEP 2 | 5 TeV |
| $ H^\dagger D_\mu H ^2$ | θ_W in M_W/M_Z | 5 TeV |
| $(H^\dagger\tau^a H)W_{\mu\nu}^a B_{\mu\nu}$ | θ_W in Z couplings | 8 TeV |
| $i(H^\dagger D_\mu\tau^a H)(\bar{L}\gamma_\mu\tau^a L)$ | Z couplings | 10 TeV |
| $i(H^\dagger D_\mu H)(\bar{L}\gamma_\mu L)$ | Z couplings | 8 TeV |
| $H^\dagger(\bar{D}\lambda_D\lambda_U\lambda_U^\dagger\gamma_{\mu\nu}Q)F^{\mu\nu}$ | $b \rightarrow s\gamma$ | 10 TeV |
| $\frac{1}{2}(\bar{Q}\lambda_U\lambda_U^\dagger\gamma_\mu Q)^2$ | B mixing | 6 TeV |

Cut-off above 10 TeV leaves $\delta m_h^2 \sim 500m_h^2$: 'little hierarchy problem'

Heavy universal new physics

Kinds of new physics

- Generic: p -decay, ν masses. see-saw, GUT
- B, L conserving: EDM, $\mu \rightarrow e\gamma$, ε_K, \dots
- Minimal Flavour Violation: $b \rightarrow s\gamma$, B -mixing, ... only SUSY?
- **'Universal'** (i.e. not coupled to fermions): \hat{S}, \hat{T}, W, Y . Little Higgs, extra d
- Effects only in Higgs: S, T . some technicolor

Heavy universal new physics

‘**Universal**’: affects only inverse propagators of vectors:

$$p^2 - M^2 + \text{SM loops} + \Pi(p^2)$$

‘**Heavy**’: expand new physics corrections $\Pi(p^2)$ as

$$\Pi(p^2) = \Pi(0) + p^2 \Pi'(0) + \frac{p^4}{2} \Pi''(0) + \dots$$

3 coefficients for each kinetic term: $\Pi_{W^+W^-}$, $\Pi_{W^3W^3}$, Π_{W^3B} , Π_{BB} .

$3 \cdot 4 = 12$ coefficients. 3 are just redefinitions of the SM parameters g, g', v .

2 combinations vanish because γ must be massless and coupled to $Q = T_3 + Y$.

| Adimensional form factors | | custodial | $SU(2)_L$ |
|---------------------------|---|-----------|-----------|
| $(g'/g)\hat{S}$ | $= \Pi'_{W^3B}(0)$ | + | - |
| $M_W^2\hat{T}$ | $= \Pi_{W^3W^3}(0) - \Pi_{W^+W^-}(0)$ | - | - |
| $-\hat{U}$ | $= \Pi'_{W^3W^3}(0) - \Pi'_{W^+W^-}(0)$ | - | - |
| $2M_W^{-2}V$ | $= \Pi''_{W^3W^3}(0) - \Pi''_{W^+W^-}(0)$ | - | - |
| $2M_W^{-2}X$ | $= \Pi''_{W^3B}(0)$ | + | - |
| $2M_W^{-2}Y$ | $= \Pi''_{BB}(0)$ | + | + |
| $2M_W^{-2}W$ | $= \Pi''_{W^3W^3}(0)$ | + | + |
| $2M_W^{-2}Z$ | $= \Pi''_{GG}(0)$ | + | + |

3 are suppressed ($V \ll \hat{U} \ll \hat{T}$ and $X \ll \hat{S}$). 5 remain: \hat{S}, \hat{T}, W, Y and Z

Final result

| Adimensional form factor | operator | effect |
|--|--|-------------------------|
| $(g'/g)\hat{S} = \Pi'_{W_3 B}(0)$ | $(H^\dagger \tau^a H) W_{\mu\nu}^a B_{\mu\nu}$ | correction to s_W |
| $M_W^2 \hat{T} = \Pi_{W_3 W_3}(0) - \Pi_{W+W-}(0)$ | $ H^\dagger D_\mu H ^2$ | correction to M_W/M_Z |
| $2M_W^{-2} Y = \Pi''_{BB}(0)$ | $(\partial_\rho B_{\mu\nu})^2/2$ | anomalous $g_1(E)$ |
| $2M_W^{-2} W = \Pi''_{W_3 W_3}(0)$ | $(D_\rho W_{\mu\nu}^a)^2/2$ | anomalous $g_2(E)$ |
| $2M_W^{-2} Z = \Pi''_{GG}(0)$ | $(D_\rho G_{\mu\nu}^A)^2/2$ | anomalous $g_3(E)$ |

(We here use canonically normalized vectors)

If the higgs exists, $\hat{S}, \hat{T}, Y, W, Z$ correspond to dimension 6 operators.

Neglected form factors (e.g. U) correspond to dimension 8 operators.

Extended H gives \hat{S}, \hat{T} . Extended vector bosons give W, Y, Z .

- \hat{S}, \hat{T} probed by comparing $s_W(M_W, M_Z)$ with $s_W(\alpha, G_F, M_Z)$ with $s_W(g_V^Z, g_A^Z)$
- W, Y probed by comparing (low E with Z -pole) and (Z -pole with LEP2).

\hat{S}, \hat{T}, W, Y **from data**

Observables: at and below the Z pole

Corrections to **Z -pole** observables from universal new physics are condensed in

$$\delta\varepsilon_1 = \hat{T} - W - Y \frac{s_W^2}{c_W^2}, \quad \delta\varepsilon_2 = -W, \quad \delta\varepsilon_3 = \hat{S} - W - Y.$$

A few observables ($M_Z, M_W, \alpha, G_F, g_{V\ell}^Z, g_{A\ell}^Z$) measured with per-mille accuracy.

Corrections to any **low-energy** observable are easily computed from

$$\mathcal{L}_{\text{eff}}(E \ll M_Z) = \mathcal{L}_{\text{QED,QCD}} - 2\sqrt{2}G_F[\bar{\nu}_L\gamma_\mu\ell_L][\bar{d}_L\gamma^\mu u_L] + \text{h.c.} +$$
$$-4\sqrt{2}G_F(1 + \hat{T}) \left[\sum_{\psi=Q,L} \bar{\psi}(T_3 - s_W^2 k Q)\gamma_\mu\psi \right]^2$$

$$k = 1 + \frac{\hat{S} - c_W^2(\hat{T} + W) - s_W^2 Y}{c_W^2 - s_W^2}.$$

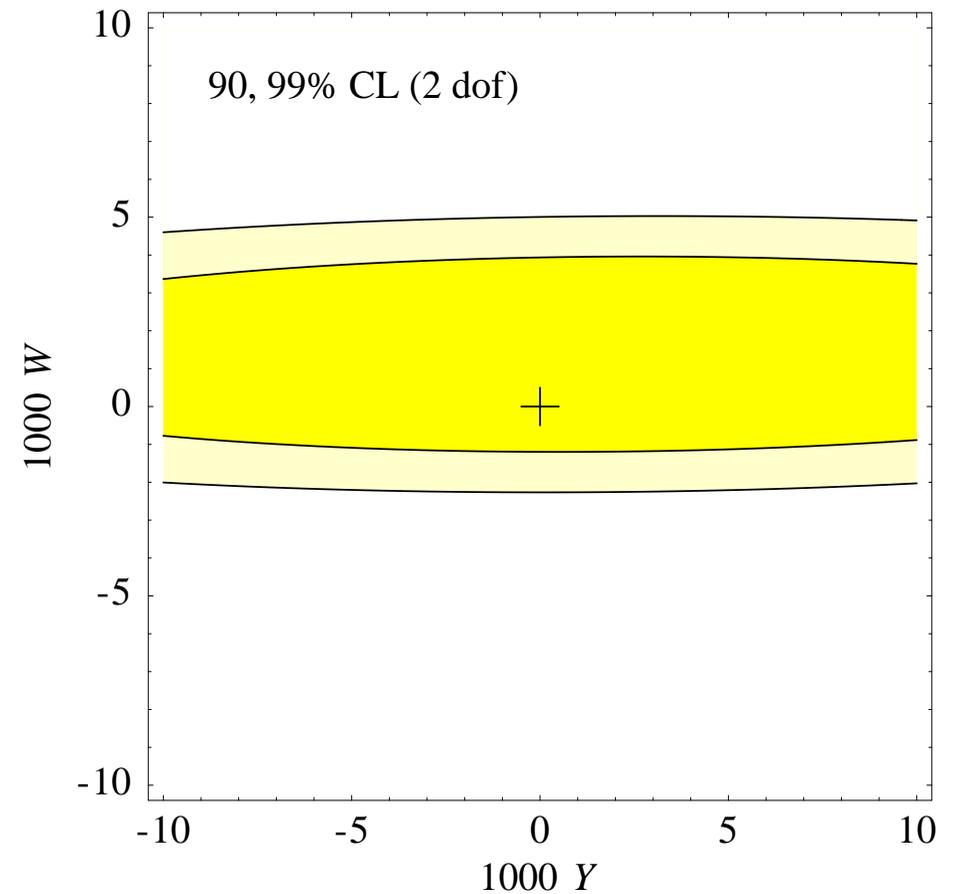
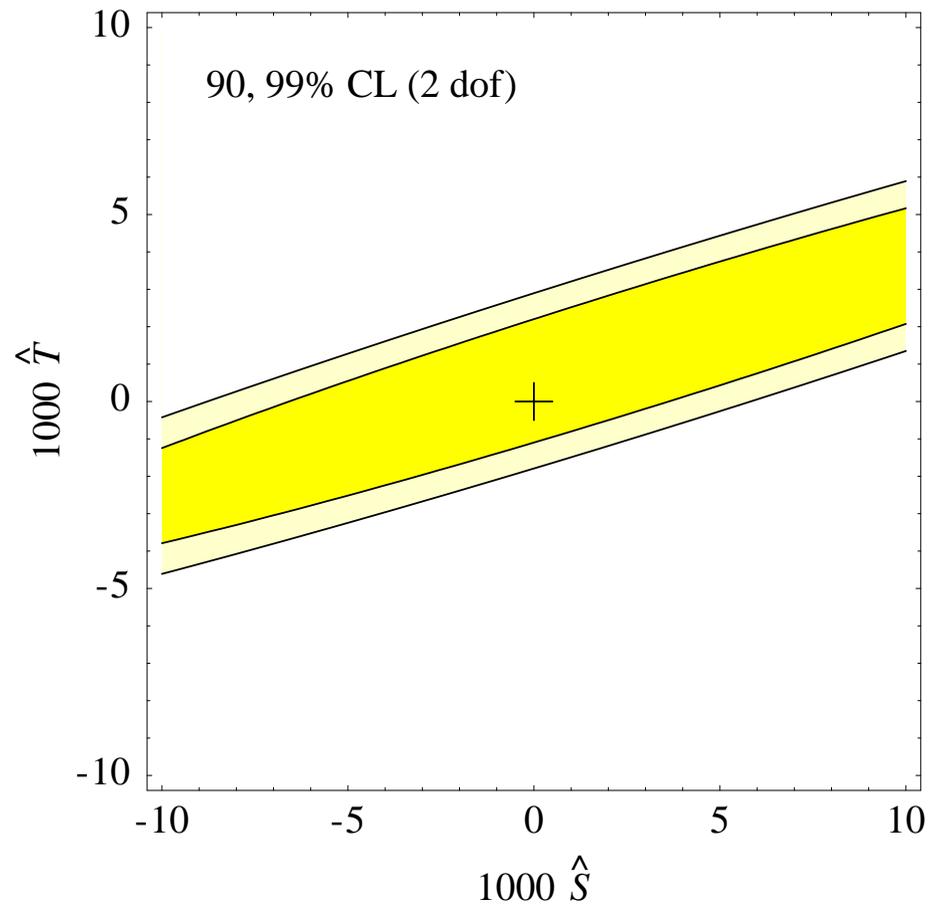
Measured with per-cent accuracy: little impact.

Global fit

Large effects still allowed

$$\chi^2(\hat{S}, \hat{T}) = \min_{W, Y} \chi^2(\hat{S}, \hat{T}, W, Y)$$

$$\chi^2(W, Y) = \min_{\hat{S}, \hat{T}} \chi^2(\hat{S}, \hat{T}, W, Y)$$

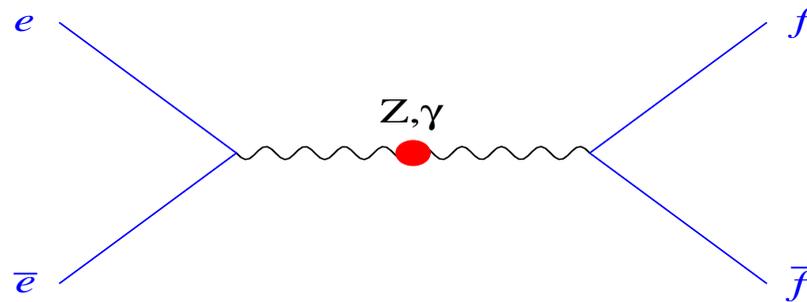


4 - 3 = 1: $\varepsilon_{1,2,3}$ give bands; adding low-energy transforms into long ellipses.

Observables: above the Z -pole

Corrections to **LEP2** $e\bar{e} \rightarrow f\bar{f}$ cross sections: use modified propagators

$$\begin{array}{c} Z \\ \gamma \end{array} \left(\begin{array}{c} \frac{1}{p^2 - M_Z^2} + \frac{\delta\epsilon_1}{p^2 - M_Z^2} - \frac{c_W^2 W + s_W^2 Y}{M_W^2} \\ - \frac{c_W^2(\delta\epsilon_1 - \delta\epsilon_2) - s_W^2 \delta\epsilon_3}{s_W c_W (p^2 - M_Z^2)} - \frac{s_W c_W (W - Y)}{M_W^2} \end{array} \right) \begin{array}{c} \\ \frac{1}{p^2} - \frac{s_W^2 W + c_W^2 Y}{M_W^2} \end{array} = \begin{array}{c} \gamma \\ \\ \end{array}$$



Measured with per-cent accuracy, but effects of W, Y enhanced by $p^2/M_Z^2 \sim 5$

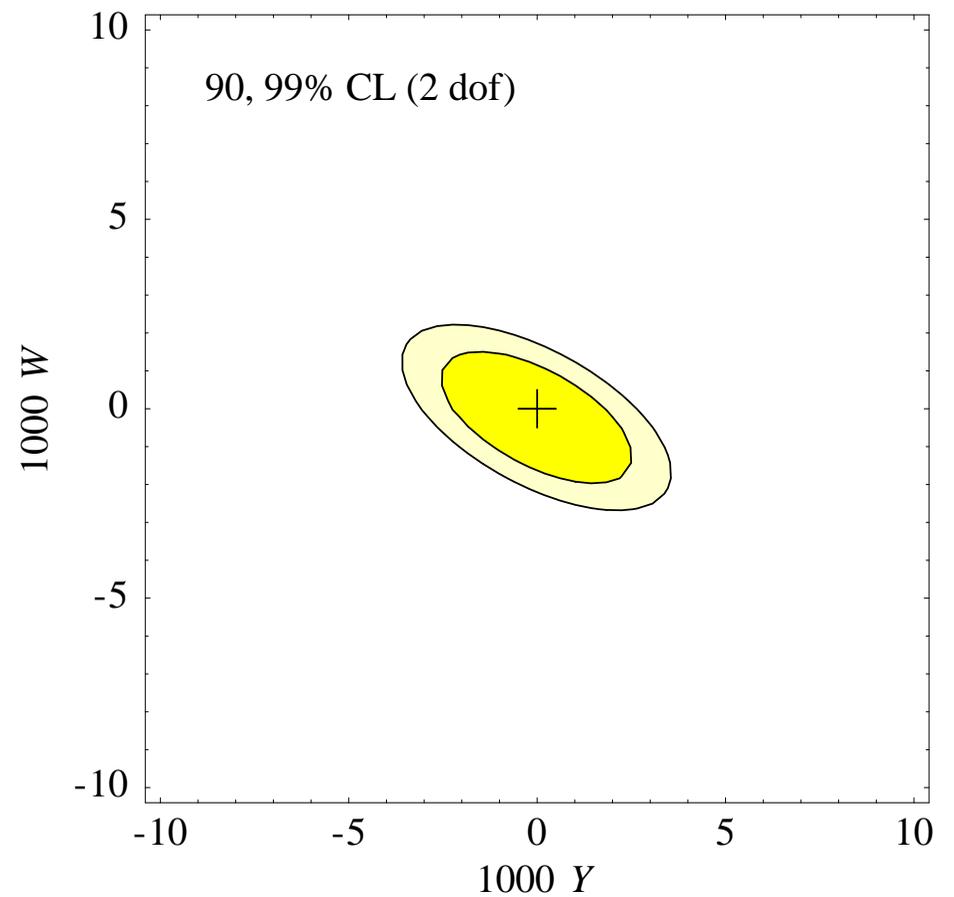
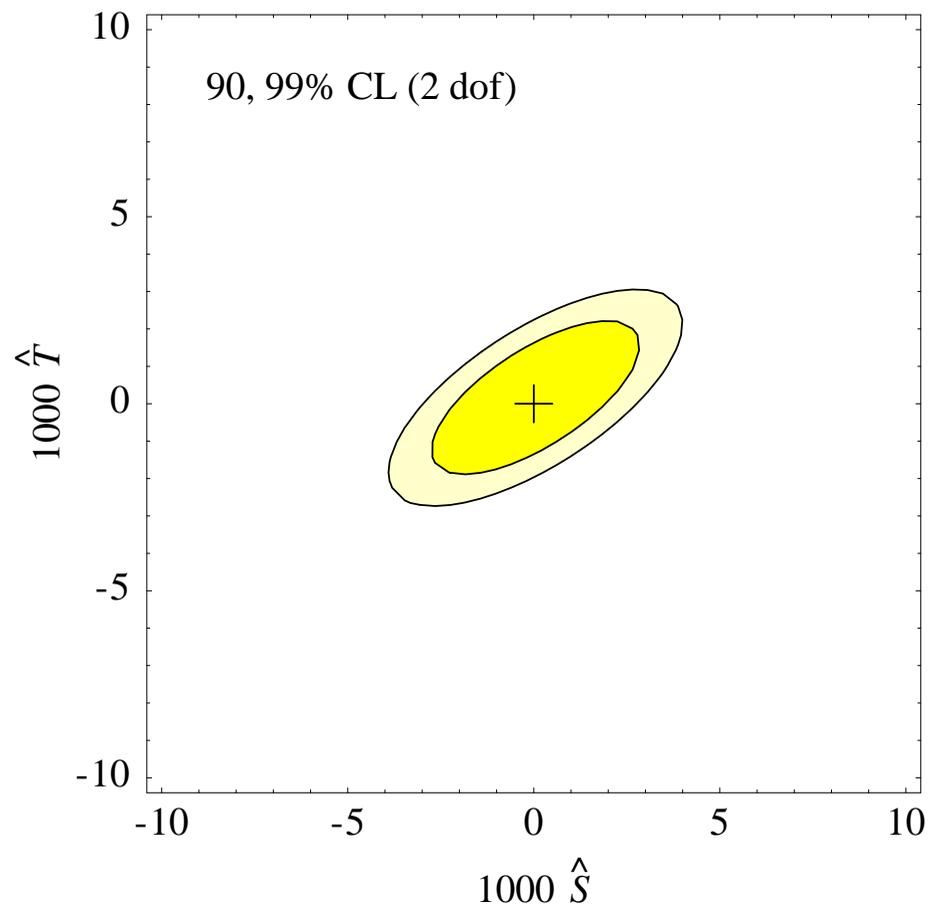
(Measurements of s_W below the Z -peak are well emphasized: APV, Møller, NuTeV. LEP2 has comparable accuracy above the Z -peak, and is missed)

Global fit after LEP2

All \hat{S}, \hat{T}, W, Y parameters must vanish within few $\cdot 10^{-3}$

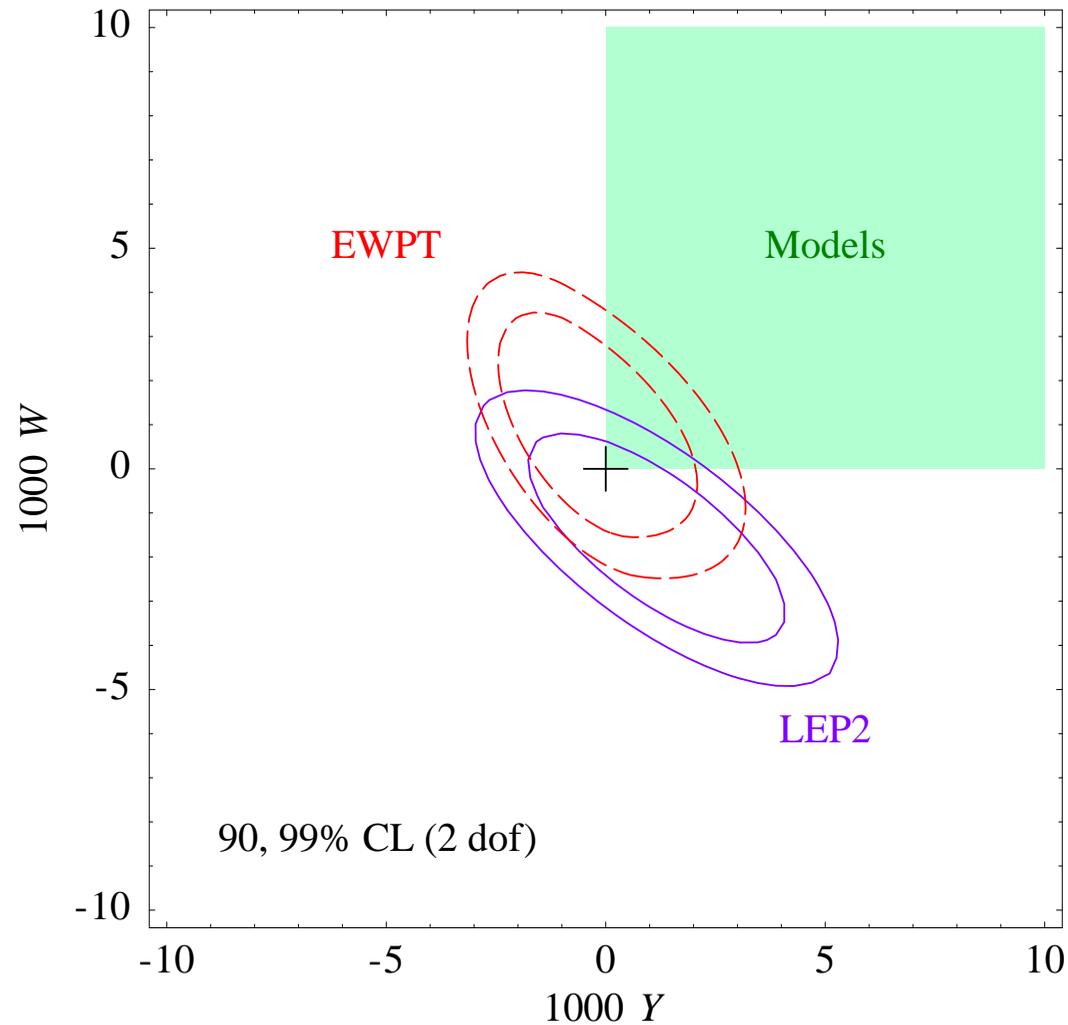
$$\chi^2(\hat{S}, \hat{T}) = \min_{W, Y} \chi^2(\hat{S}, \hat{T}, W, Y)$$

$$\chi^2(W, Y) = \min_{\hat{S}, \hat{T}} \chi^2(\hat{S}, \hat{T}, W, Y)$$



Hard time for Higgsless, little-Higgs etc.

LEP1 vs LEP2: $\chi^2(\hat{S} = 0, \hat{T} = 0, W, Y)$



LEP2 relevant and shifts towards $W < 0$. Models give $W, Y \geq 0$
Precise analysis by LEP2 experimentalists would be welcome

Universal models

Hidden universal models

Popular models (vectors in extra dimensions, little-Higgs, ...) have extra heavy vectors coupled to SM fermionic gauge currents J_F .

Integrating out heavy vector mass eigenstates gives additional operators:

$$\mathcal{O} \sim (J_F + J_H)^2 = (\bar{\psi}\gamma_\mu\psi + iH^\dagger D_\mu H)^2 = \begin{cases} \text{4-fermion operators} \\ \text{corrections to } Z, W, \gamma \text{ couplings} \\ \text{corrections to } Z, W, \gamma \text{ masses} \end{cases}$$

Looks non-universal, so analyses performed by computing all observables. A posteriori can be rewritten as universal: e.g. on shell $J_\mu^B J_\mu^B = (\partial_\alpha B_{\mu\nu})^2/2 \rightarrow Y$.

How to skip superfluous steps putting a priori effects in SM vector propagators?

$$\frac{1}{p^2 - m_{\text{SM}}^2} \rightarrow \frac{1}{p^2 - m_{\text{SM}}^2} + \frac{1}{p^2 - m_{\text{new}}^2}$$

How to compute \hat{S}, \hat{T}, W, Y

Do not integrate out the heavy vector mass eigenstates.

Integrate out vector bosons not coupled to SM fermions.

- ★ Apparently non-universal operators involving fermions not generated.
- ★ No need of diagonalizing and indentifying heavy mass eigenstates.

It works like a pig → sausage machine:

- 1) Choose a model; write kinetic matrix Π_{ij}^{full} of neutral (W_3, B, \dots) and charged (W^\pm, \dots) vectors. (... indicates extra vectors not coupled to SM fermions)
- 2) $\Pi^{-1} = (\Pi^{\text{full}})^{-1}$ restricted to SM vectors
- 3) Extract \hat{S}, \hat{T}, W, Y from Π
- 4) Compare with $\chi^2(\hat{S}, \hat{T}, W, Y)$

A simple example: $U(1)_Y \otimes U(1)'_Y$

Extra hypercharge vector with mass M not mixed with SM.

1) Kinetic matrix:

$$\Pi^{\text{full}} = \begin{matrix} & B_\mu & W_\mu^3 & B'_\mu \\ \begin{matrix} B_\mu \\ W_\mu^3 \\ B'_\mu \end{matrix} & \begin{pmatrix} p^2 - M_Z^2 s_W^2 & M_Z^2 s_W c_W & 0 \\ M_Z^2 s_W c_W & p^2 - M_Z^2 c_W^2 & 0 \\ 0 & 0 & p^2 - M^2 \end{pmatrix} \end{matrix}$$

2) Integrate out $B_\mu - B'_\mu$ not coupled to fermions: go to the basis $(B, W^3, B - B')$, invert Π^{full} and restrict to B, W^3 : the result of course is

$$\Pi^{-1} = \begin{pmatrix} p^2 - M_Z^2 s_W^2 & M_Z^2 s_W c_W \\ M_Z^2 s_W c_W & p^2 - M_Z^2 c_W^2 \end{pmatrix}^{-1} + \begin{pmatrix} 1/(p^2 - M^2) & 0 \\ 0 & 0 \end{pmatrix}$$

3) Extract $\hat{S} = Y = \hat{T}/t_W^2 = M_W^2/M^2$, $W = 0$. LEP1 not affected: $\delta\epsilon_{1,2,3} = 0$

Gauge bosons in extra dimension

Kaluza-Klein vectors are like $G \otimes G \otimes G \dots$ with masses $M = 1/R, 2/R, 3/R \dots$



Vectors and higgs in 5d; fermions localized on a brane: pig machine produces

$$\frac{1}{\Pi} = \sum_{n=-\infty}^{+\infty} \frac{1}{p^2 - n^2/R^2} = \text{brane to brane propagator}$$

$$\Pi = \frac{p}{\pi R} \tan p\pi R \simeq p^2 + \frac{p^4}{3} \pi^2 R^2 + \dots$$

KK of $SU(2)_L$ bosons produce W , B_μ KK give Y , gluons KK give Z :

$$W = Y = Z = \frac{\pi^2}{3} M_W^2 R^2.$$

Without LEP2: $1/R > 4.5$ TeV. With LEP2: $1/R > 6.4$ TeV. At 95% CL.

If instead the higgs is localized together with fermions, then one gets also

$$\hat{S} = \frac{\pi^2}{6} M_W^2 R^2 \tan \theta_W, \quad \hat{T} = \frac{\pi^2}{3} M_W^2 R^2 \tan^2 \theta_W.$$

Without LEP2: $1/R > 3.8$ TeV. With LEP2: $1/R > 6.3$ TeV. At 95% CL.

Little Higgs

Higgs as pseudo-Goldstone

Basic idea:

Higgs is a pseudo-Goldstone boson of a global symmetry broken at a scale f

Happens in QCD, making π lighter than proton.
Solved doublet/triplet problem of SUSY-SU(5).

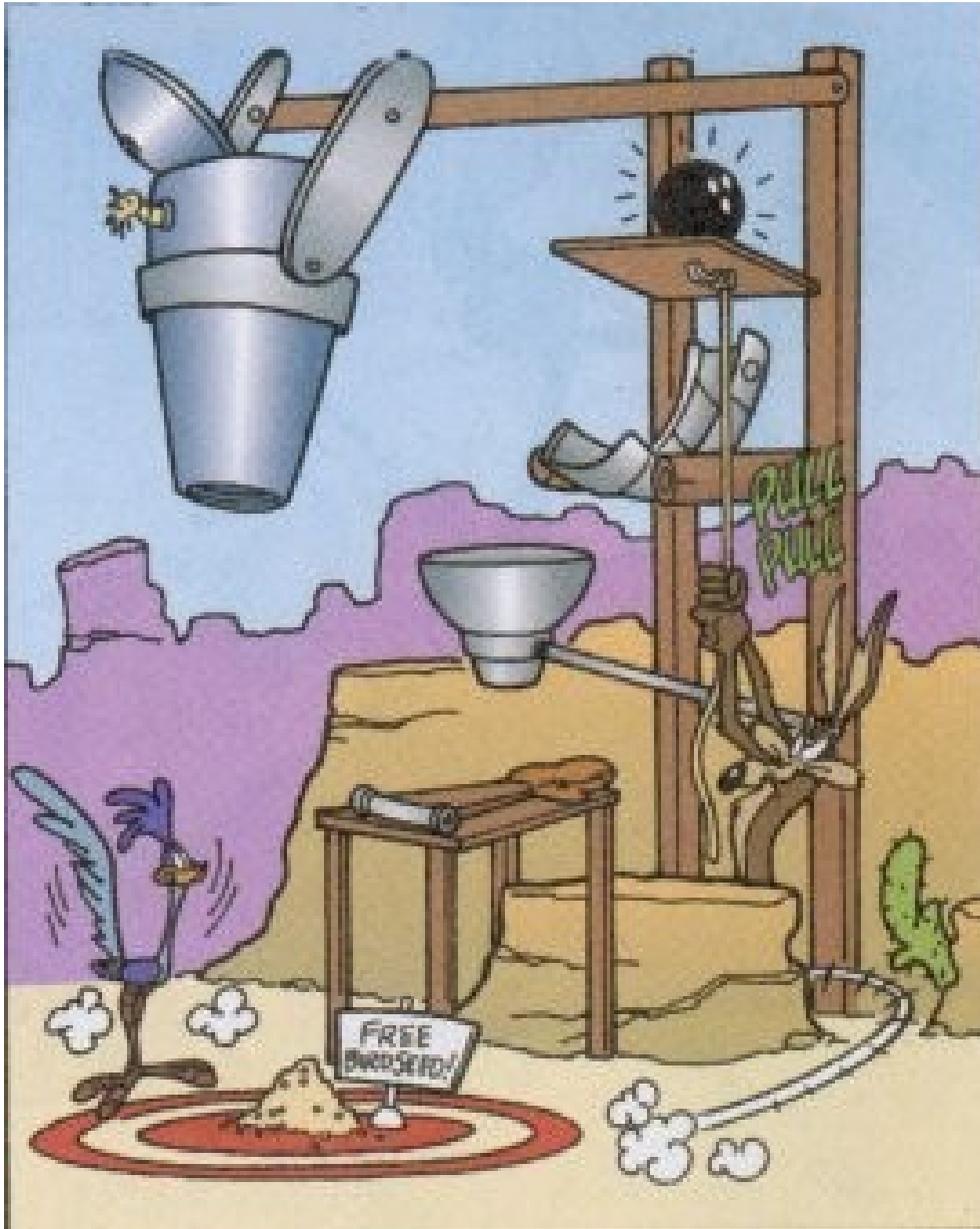
But

The Higgs seems not a Goldstone boson:

- a Goldstone boson π has flat potential: $V \sim 0\pi^2 + 0\pi^4$.
- we want a small Higgs mass, but we need a sizable coupling: $V \sim 0h^2 + \lambda h^4$.

To proceed anyway one needs to build complex machineries: little Higgs models

The little-Higgs mechanism



← A global symmetry contains **two copies of the electroweak gauge group**, spontaneously broken to the SM at scale f by more than a single Higgs field. As in D/T models the top Yukawa can be obtained by mixing with extra vector tops.

← Basic idea

Little Higgs models

| global | gauge | \hat{S} | \hat{T} | W | Y |
|--------------------|-------|---|---|--|---|
| SU(5) | 32211 | $\frac{2M_W^2}{g^2 f^2} \left[\cos^2 \phi + 5 \frac{c_W^2}{s_W^2} \cos^2 \phi' \right]$ | $\frac{5M_W^2}{g^2 f^2} + \hat{T}_{\text{triplet}}$ | $\frac{4M_W^2}{g^2 f^2} \cos^4 \phi$ | $\frac{20M_W^2}{g'^2 f^2} \cos^4 \phi'$ |
| SU(5) | 3221 | $\frac{2M_W^2}{g^2 f^2} \cos^2 \phi$ | $0 + \hat{T}_{\text{triplet}}$ | $\frac{4M_W^2}{g^2 f^2} \cos^4 \phi$ | 0 |
| SO(9) | 32221 | $\frac{2M_W^2}{g^2 f^2} \left[\cos^2 \phi_L + \frac{c_W^2}{s_W^2} \cos^2 \phi_R \right]$ | $0 + \hat{T}_{\text{triplet}}$ | $\frac{4M_W^2}{g^2 f^2} \cos^4 \phi_L$ | $\frac{4M_W^2}{g'^2 f^2} \cos^4 \phi_R$ |
| SU(6) | 32211 | $\frac{2M_W^2}{g^2 f^2} \left[\cos^2 \phi + 2 \frac{c_W^2}{s_W^2} \cos^2 \phi' \right]$ | $\frac{M_W^2}{2g^2 f^2} (5 + \cos 4\beta)$ | $\frac{4M_W^2}{g^2 f^2} \cos^4 \phi$ | $\frac{8M_W^2}{g'^2 f^2} \cos^4 \phi'$ |
| SU(6) | 3221 | $\frac{2M_W^2}{g^2 f^2} \cos^2 \phi$ | $\frac{M_W^2}{g^2 f^2} \cos^2 2\beta$ | $\frac{4M_W^2}{g^2 f^2} \cos^4 \phi$ | 0 |
| SU(3) ² | 331 | $\approx \frac{2M_W^2}{f^2 g^2}$ | ≈ 0 | $\approx \frac{M_W^2}{2f^2 g^2}$ | $\approx \frac{g'^2 M_W^2}{2f^2 g^4}$ |

$\tan \phi = g_2/g_1$, $\tan \phi' = g'_2/g'_1$, $\tan \phi_L = g_L/g_2$, $\tan \phi_R = g_R/g_1$, $\tan \beta = v_2/v_1$

All f normalized such that non-abelian vectors have masses $M^2 = g^2 f^2/4$.

32211 is a shorthand for $SU(3) \otimes SU(2)_1 \otimes SU(2)_2 \otimes U(1)_2 \otimes U(1)_1$, etc

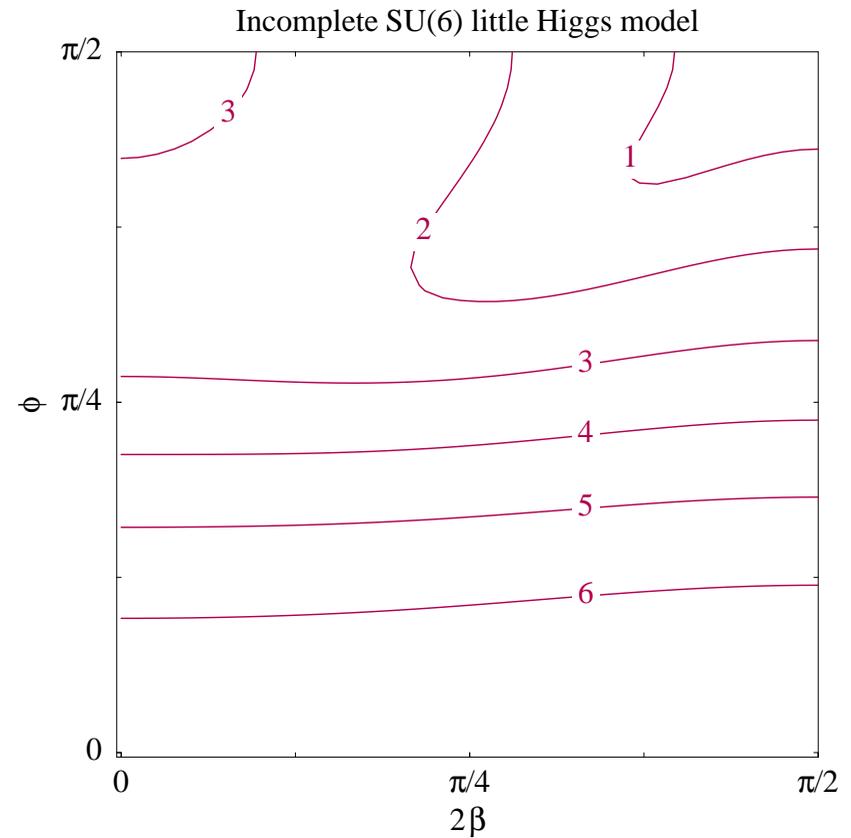
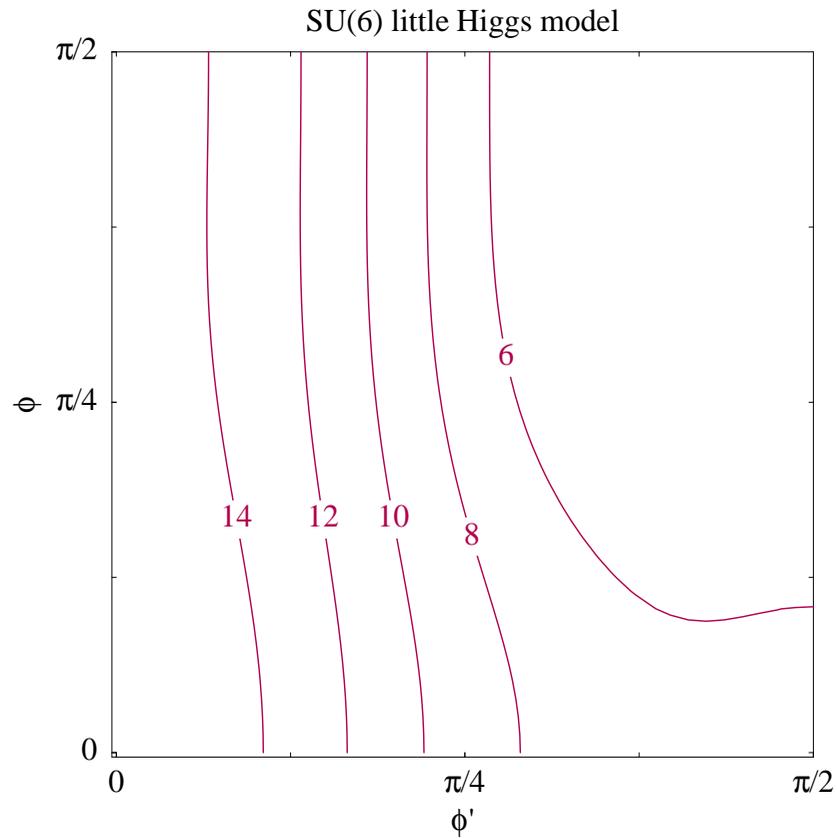
Some models have Higgs triplets with vev v_T : $\hat{T}_{\text{triplet}} = -g^2 v_T^2 / M_W^2$.

Various disagreements with previous analyses

We will plot 99% C.L. bounds on f i.e. $\chi^2 = \chi_{\text{SM}}^2 + 6.6$ (1 d.o.f!)

We assume light higgs. Heavy higgs allowed in models with $\hat{T} \sim +\text{few} \cdot 10^{-3}$.

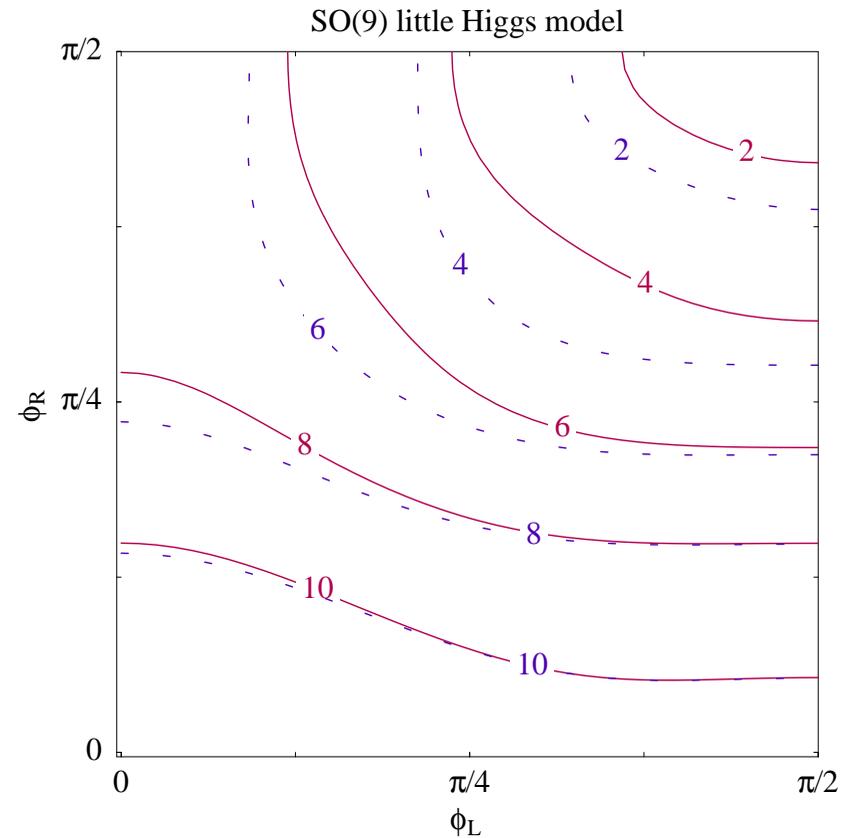
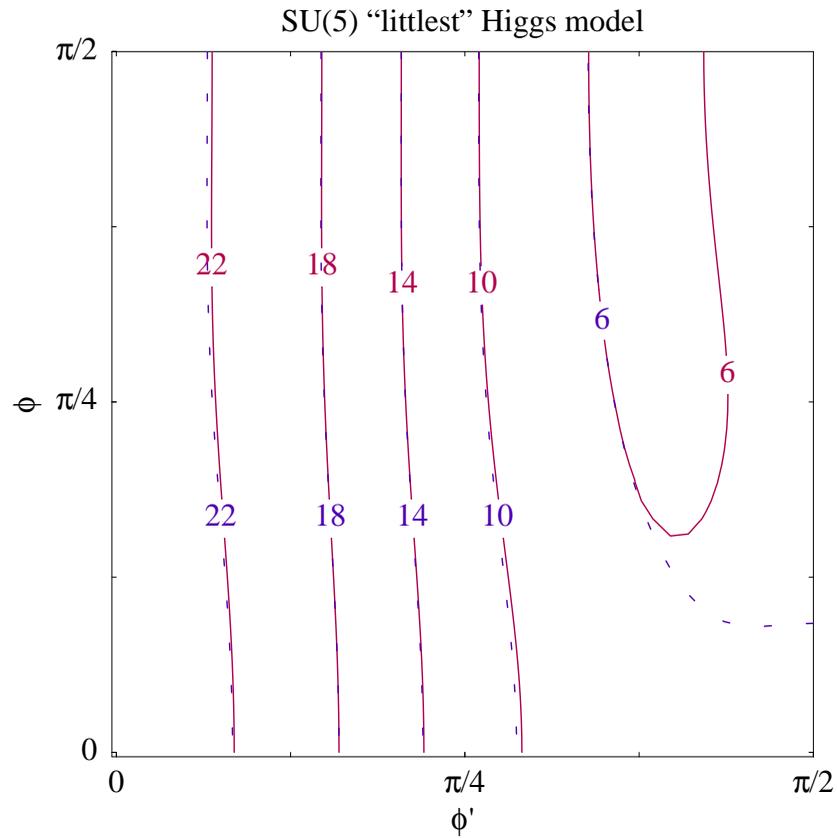
Models without Higgs triplets



Strongest constraint from extra U(1).

Dropping it the model becomes less constrained but incomplete: $\delta m_h^2 \sim g'^2 \Lambda^2$.

Models with Higgs triplets



Constraint slightly relaxed by an extra \hat{T} (negative in SU(5), positive in SO(9))

Little Higgs and precision data

All indirect effects condensed in 4 observables: \hat{S}, \hat{T}, W, Y .

Not enough to indirectly test models with 4 free parameters.

Nevertheless models predict inequalities, some common to all models:

$$W, Y \geq 0, \quad S > (W + Y)/2 \quad \hat{T} \dots$$

- $\hat{T} = 0$ in models with custodial $SU(2)_R$ or with a single $U(1)$
- $Y = 0$ in 'incomplete' models with a single $U(1)$

Above models are fine-tuned: $f > \text{few TeV}$ and $FT \sim (f/v)^2 \sim 100 \div 1000$

Sometimes constraint on f stronger than LHC sensitivity.

'Simplest' little Higgs

Basic idea: $SU(3) \otimes U(1)_X \xrightarrow{f} SU(2)_L \otimes U(1)_Y$ by **two** $SU(3)$ Higgs triplets $H_{1,2}$
(Or a triplet H and an adjoint Σ as in old models for doublet/triplet splitting).

Forbidding $|H_1 H_2|^2$ or $H \Sigma \Sigma^* H$ gives a $SU(3) \otimes SU(3)$ global symmetry.

The light Higgs doublet is its pseudo-Goldstone boson.

Non universal corrections to precision observables from an extra Z' boson

$$M_{Z'}^2 = \frac{2g^2}{3c_{Z'}^2} f^2 \approx 0.24 f^2 \quad g_{Z'} = \frac{g}{c_{Z'}} \approx 0.60, \quad Z' \text{ charge} = T_8 + \sqrt{3} s_{Z'} Y$$

Corrections to most precise precision data described by

$$\hat{S} = 4W = \frac{2M_W^2}{f^2 g^2} = \frac{4Y}{\tan^2 \theta_W}, \quad \hat{T} = 0$$

$$f > 4.5 \text{ TeV at } 99\% \text{ CL.}$$

Generic Z'

Non universal. Specified by $M_{Z'}$, $g_{Z'}$ and by charges Z'_H , $Z'_{L_{1,2,3}}$, $Z'_{E_{1,2,3}}$, ...

A simple approximation holds if e, μ, τ have the same Z' charge:
restrict to charged leptons, better probed than quarks or neutrinos.

Done by integrating out combination not coupled to e_L and e_R :

$$B_\mu \rightarrow B_\mu - c_Y Z'_\mu, \quad W_\mu^3 \rightarrow W_\mu^3 - c_W Z'_\mu$$

$$c_Y = \frac{g_{Z'} Z'_E}{g' Y_E}, \quad c_W = \frac{2g_{Z'}}{Y_E g} (Z'_E Y_L - Z'_L Y_E)$$

Get

$$\hat{S} = \frac{M_W^2}{M_{Z'}^2} (c_W - c_Y/t)(c_W - c_Y t - 2g_{Z'} Z'_H/g), \quad W = \frac{M_W^2}{M_{Z'}^2} c_W^2,$$

$$\hat{T} = \frac{M_W^2}{M_{Z'}^2} [(c_Y t + 2g_{Z'} Z'_H/g)^2 - c_W^2], \quad Y = \frac{M_W^2}{M_{Z'}^2} c_Y^2.$$

Higgsless models

Without the Higgs unitarity lost at $E \gtrsim 4\pi v \sim \text{TeV}$

Some 5d models try to maintain unitarity up to $E \sim (4\pi)^2 v/g \sim 10 \text{ TeV}$.

Proposed models are ‘universal’ and give (with fermions on a brane)

$$\hat{S} \sim \frac{\alpha}{4\pi} \frac{1}{\epsilon_5} \quad \epsilon_5 \text{ is a 5d loop expansion factor}$$

- If $\epsilon_5 \sim 1$ the model is uncomputable (‘not even wrong’)
- If $\epsilon_5 \ll 1$ the model is excluded, because after LEP2 $|\hat{S}| \ll 0.01$.

Universal extra dimensions

With all SM fields in extra dimensions there are no *computable* tree level effects.

Usual conclusion: $1/R \sim v$ is allowed.

But:

1) More structure (orbifolds...) needed to get chiral 4d fermions from extra dim.s: loop effects are ∞ because they do not respect the tree level setup.

2) More generically, gauge interactions are renormalizable only in 4d ($[g] = 0$): in higher dimension why only would-be renormalizable terms should be present?

Adding higher order operators the reasonable constraint is $1/R > \mathcal{O}(10 \text{ TeV})$.

Additional problems when applied to

Higgsless: why data reproduce SM with light Higgs if there is no Higgs?

Little Higgs with T parity: small $f \sim v$ stabilizes v but new f hierarchy problem.

Supersymmetry

LEP2 indirect data and SUSY

LEP2 saw $N \sim 10^4$ $e\bar{e} \rightarrow f\bar{f}$ events at $\sqrt{s} = 200$ GeV.

So LEP2 is sensitive to $\mathcal{O} = \frac{4\pi}{\Lambda^2}(\bar{e}\gamma_\mu e)(\bar{f}\gamma_\mu f)$ up to $\Lambda \gtrsim \sqrt{\frac{sN^{1/2}}{\alpha}} \approx 10$ TeV.

Indeed LEP2 collaborations claim $\Lambda \gtrsim 10$ TeV.

Sparticles of mass m_{SUSY} generate \mathcal{O} with $4\pi/\Lambda^2 \sim g^4/(4\pi m_{\text{SUSY}})^2$.

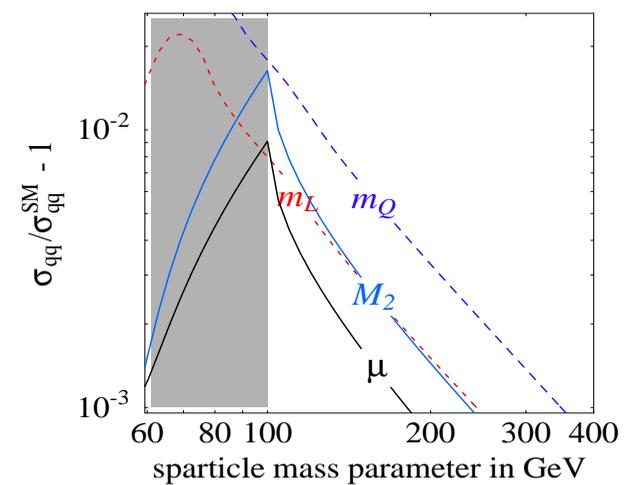
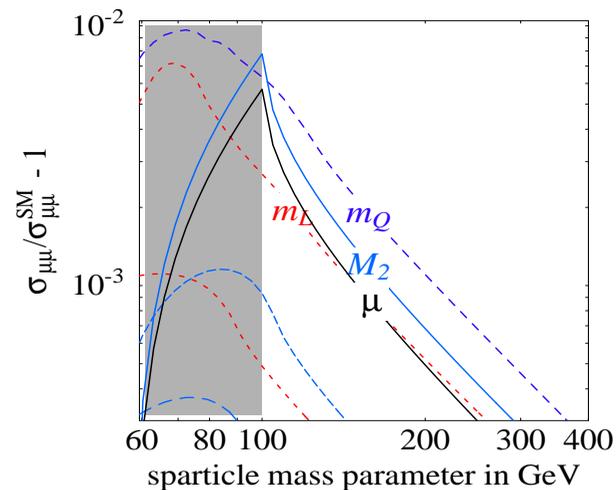
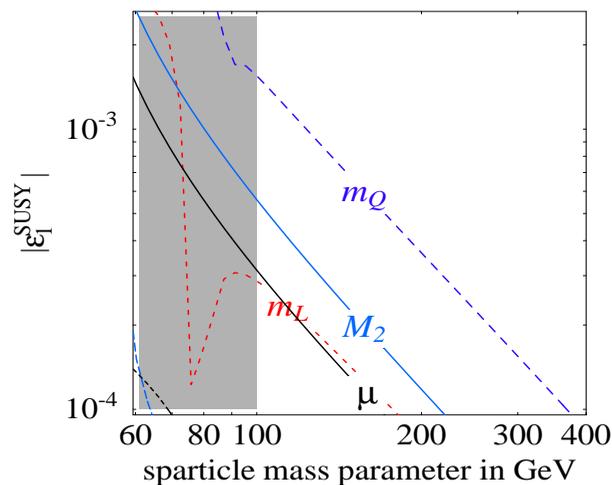
So $m_{\text{SUSY}} \gtrsim g^2\Lambda/(4\pi)^{3/2} \approx 100$ GeV, comparable to direct bounds.

[Years ago attempt with Gambino and Giudice failed because too complex. Now \hat{S}, \hat{T}, W, Y approximation allowed to understand and proceed correctly].

SUSY is neither universal nor heavy

1) SUSY is not universal: corrections to propagators, vertices and boxes are comparable. Actually only corrections to propagators are cumulative in the number of generations, colors, isospin: **the universal approximation is good within $1/N_{\text{gen}} \sim 30\%$.** And SUSY becomes exactly universal if fermionic sparticles are lighter than scalar sparticles ('split' SUSY limit) and in the opposite limit.

2) SUSY is not heavy. Actually $\tilde{m} > 100 \text{ GeV}$ so that at LEP1 the **heavy approximation is good within $(M_Z/2\tilde{m})^2 \lesssim 25\%$.** At LEP2 it misses the resonant enhancement of fermionic sparticles:



Sfermions and Higgs bosons

$$\hat{S} = -\frac{\alpha_2}{24\pi} \left[M_W^2 \left(-\frac{1}{6m_L^2} + \frac{3}{2m_Q^2} \right) \cos 2\beta + \frac{1}{2} \frac{m_t^2}{m_Q^2} + \frac{M_W^2}{2m_A^2} \left(1 - \frac{M_Z^2}{2M_W^2} \sin^2 2\beta \right) \right]$$

$$\hat{T} = \frac{\alpha_2}{16\pi} M_W^2 \cos^2 2\beta \left(\frac{1}{m_L^2} + \frac{2}{m_Q^2} \right) + T_{\text{stop}} + \frac{\alpha_2}{48\pi} \frac{M_W^2}{m_A^2} \left(1 - \frac{M_Z^2}{M_W^2} \sin^2 2\beta \right)$$

$$Y = \frac{\alpha_Y}{40\pi} M_W^2 \left(\frac{1}{m_E^2} + \frac{1}{2m_L^2} + \frac{1}{3m_D^2} + \frac{4}{3m_U^2} + \frac{1}{6m_Q^2} + \frac{1}{6m_A^2} \right),$$

$$W = \frac{\alpha_2}{80\pi} M_W^2 \left(\frac{1}{m_L^2} + \frac{3}{m_Q^2} + \frac{1}{3m_A^2} \right)$$

where $T_{\text{stop}} \approx +\frac{\alpha_2}{16\pi} \frac{(m_t + M_W \cos 2\beta)^2}{m_{Q3}^2 M_W^2}$ can be better approximated.

Gauginos and higgsinos

$$\hat{S} \approx \frac{\alpha_2 M_W^2}{12\pi M_2^2} \left[\frac{r(r-5-2r^2)}{(r-1)^4} + \frac{1-2r+9r^2-4r^3+2r^4}{(r-1)^5} \ln r \right] + \frac{\alpha_2 M_W^2}{24\pi M_2 \mu} \left[\frac{2-19r+20r^2-15r^3}{(r-1)^4} + \frac{2+3r-3r^2+4r^3}{(r-1)^5} 2r \ln r \right] \sin 2\beta,$$

$$\hat{T} \approx \frac{\alpha_2 M_W^2}{48\pi M_2^2} \left[\frac{7r-29+16r^2}{(r-1)^3} + \frac{1+6r-6r^2}{(r-1)^4} 6 \ln r \right] \cos^2 2\beta,$$

$$Y = \frac{\alpha_Y M_W^2}{30\pi \mu^2},$$

$$W = \frac{\alpha_2}{30\pi} \left[\frac{M_W^2}{\mu^2} + \frac{2M_W^2}{M_2^2} \right]$$

having neglected $s_W^2 \approx 0$ in \hat{S}, \hat{T} and defined $r = \mu^2/M_2^2$.

Unlike W and Y , \hat{S} and \hat{T} are suppressed by $1/\max(\mu, M_2)^2$.

General features

Precision tests compared to $g - 2$, $b \rightarrow s\gamma$, $B_s \rightarrow \mu\bar{\mu}$, m_h , DM

- Insensitive to model details (e.g. NMSSM drastically affects m_h and DM)
- Featureless: no big enhancements nor suppressions (e.g. large $\tan\beta$, coann)
- $W, Y > 0$ can cumulate up to observable level. (LEP2 prefers $W < 0$).
- Depend almost only on few main parameters: $M_2, m_Q, m_L, \mu, \dots A_t, \tan\beta \dots$

| | CMSSM at M_{GUT} | Gauge mediation at 10^{10} GeV | Anomaly + radion mediation |
|-------------------|------------------------------|--|---------------------------------|
| M_2 | $0.82M_{1/2}$ | $0.82\tilde{M}_{1/2}$ | $-0.43M_{\text{AM}}$ |
| m_Q^2 | $m_0^2 + 6.2M_{1/2}^2$ | $6.5\tilde{m}_0^2 + 5.2\tilde{M}_{1/2}^2$ | $m_0^2 + 16M_{\text{AM}}^2$ |
| m_L^2 | $m_0^2 + 0.52M_{1/2}^2$ | $1.3\tilde{m}_0^2 + 0.24\tilde{M}_{1/2}^2$ | $m_0^2 - 0.37M_{\text{AM}}^2$ |
| $\mu^2 + M_Z^2/2$ | $0.17m_0^2 + 2.6M_{1/2}^2$ | $2.9\tilde{m}_0^2 + 1.7\tilde{M}_{1/2}^2$ | $0.17m_0^2 + 10M_{\text{AM}}^2$ |

- $(m_0, M_{1/2})$ -like plots are representative (not only sample slices)

Split SUSY

Universal: simple warming exercise, motivated by anthropic arguments: v small so that we form. Λ small so that we survive. M_2, μ small so that we work.

Only M_2 light.

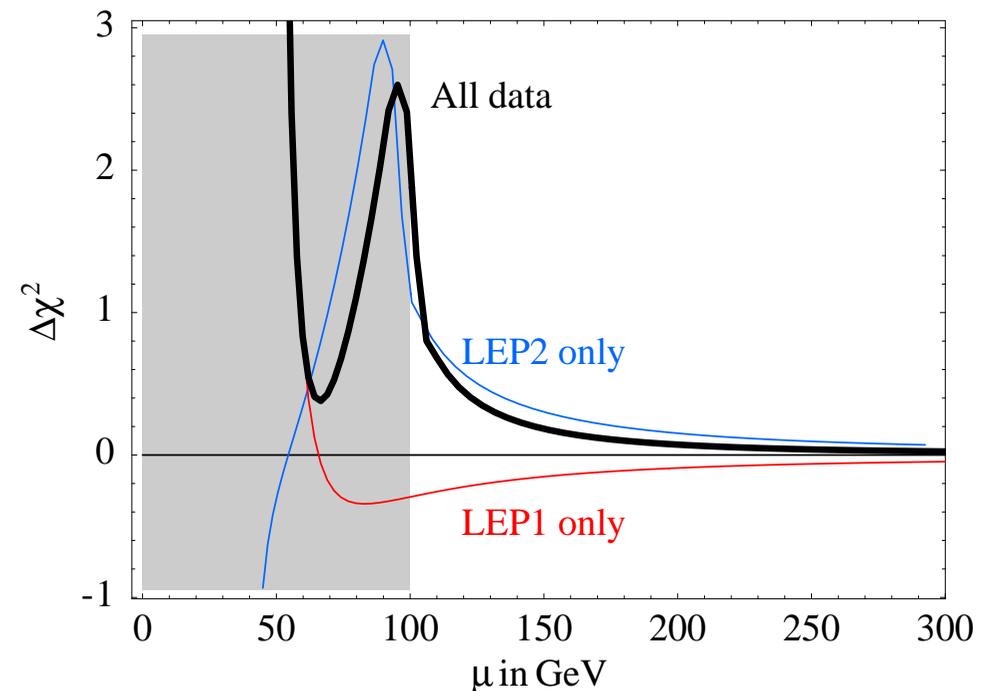
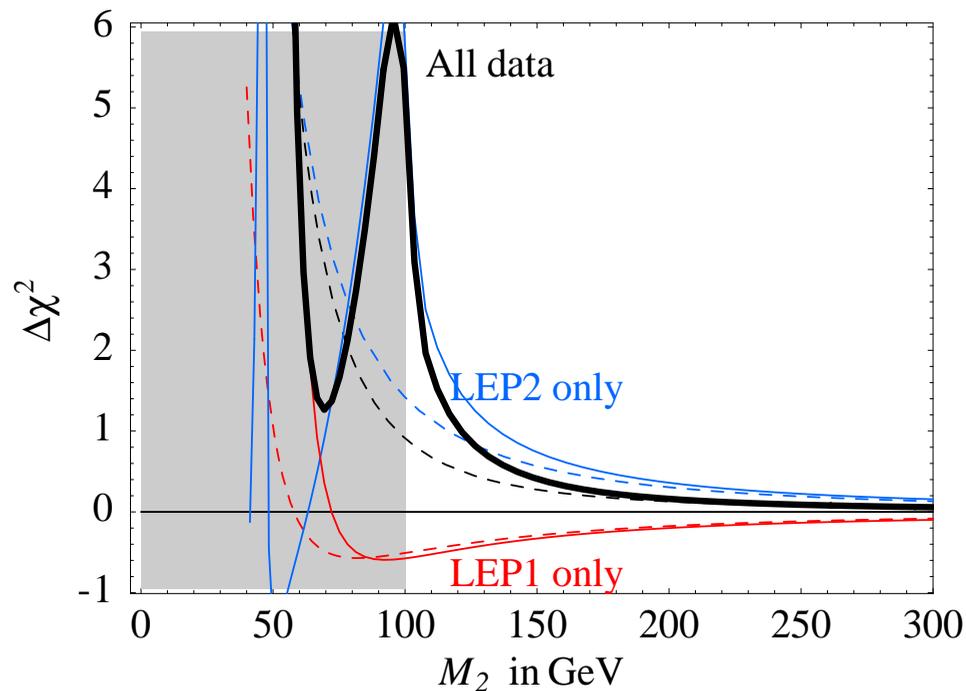
$$\hat{S} = \hat{T} = Y \simeq 0,$$

$$W \simeq \frac{\alpha_2}{15\pi} \frac{M_W^2}{M_2^2}$$

Only μ light.

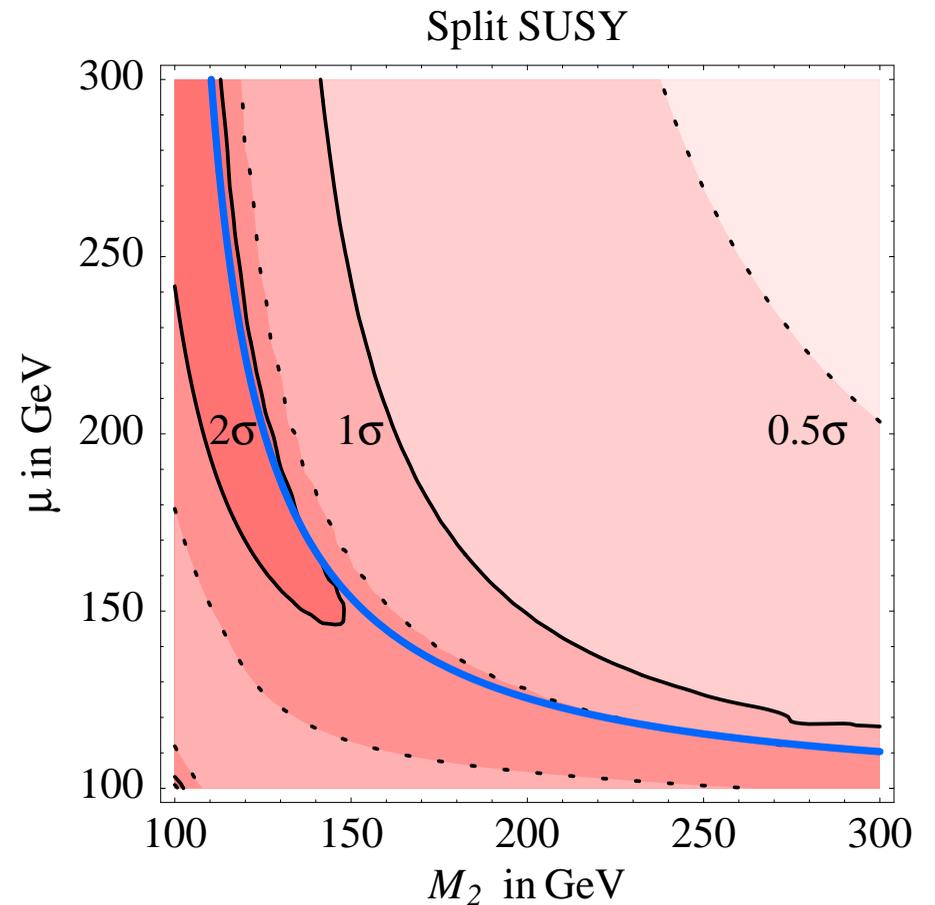
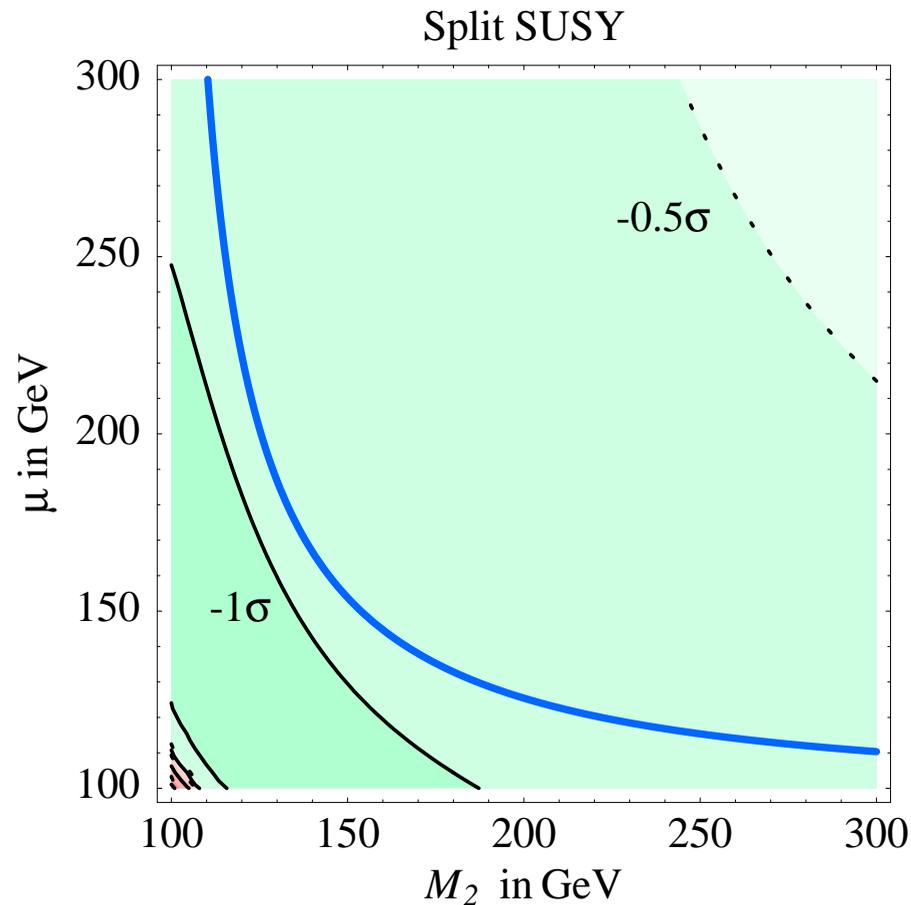
$$\hat{S} = \hat{T} \simeq 0,$$

$$W \simeq Y \simeq \frac{\alpha_2}{30\pi} \frac{M_W^2}{\mu^2}.$$



Split SUSY

($\tan \beta = 10$, gaugino unification)



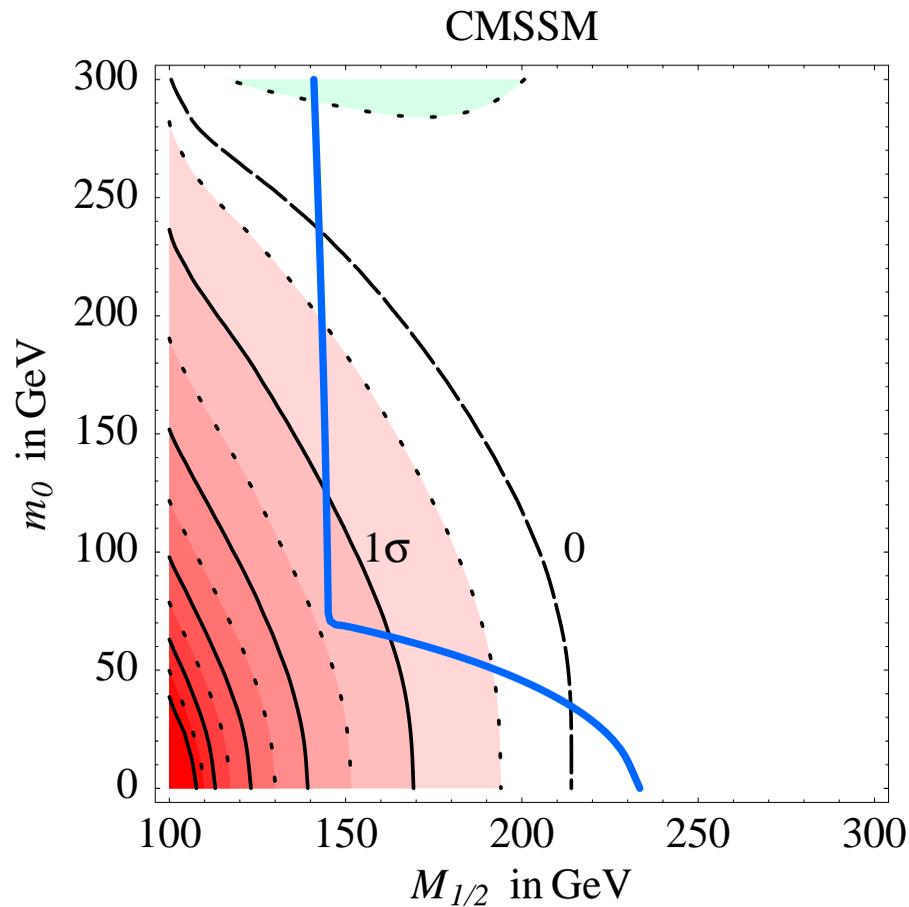
Without LEP2: mildly favoured

With LEP2: mildly disfavoured

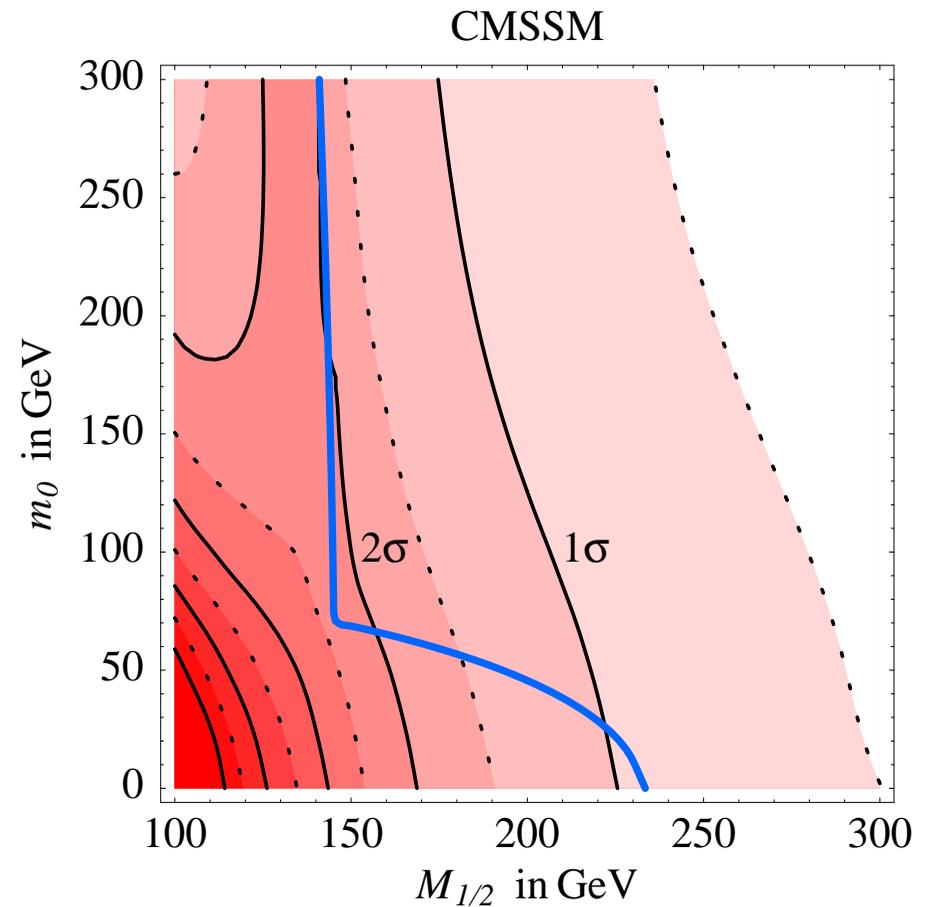
The thick blue line is the direct constraint $m_\chi, m_{\tilde{\ell}} > 100$ GeV

The CMSSM

($\tan \beta = 10$, $A_0 = 0$, $\mu > 0$)



Without LEP2

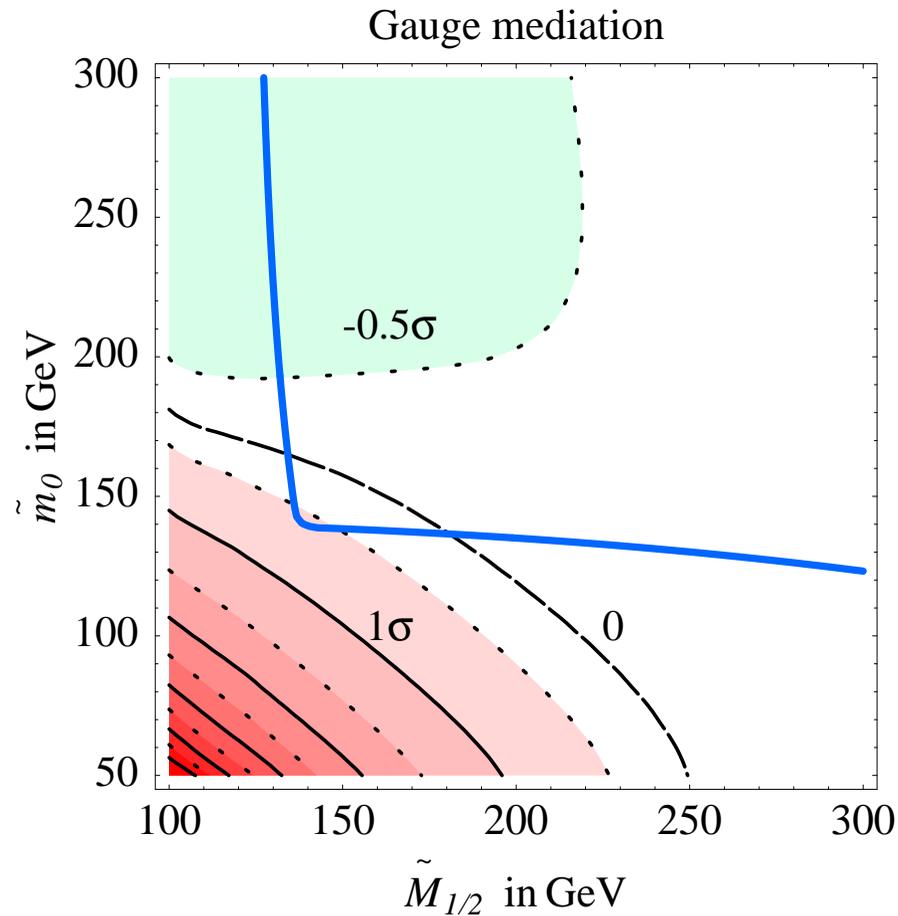


With LEP2

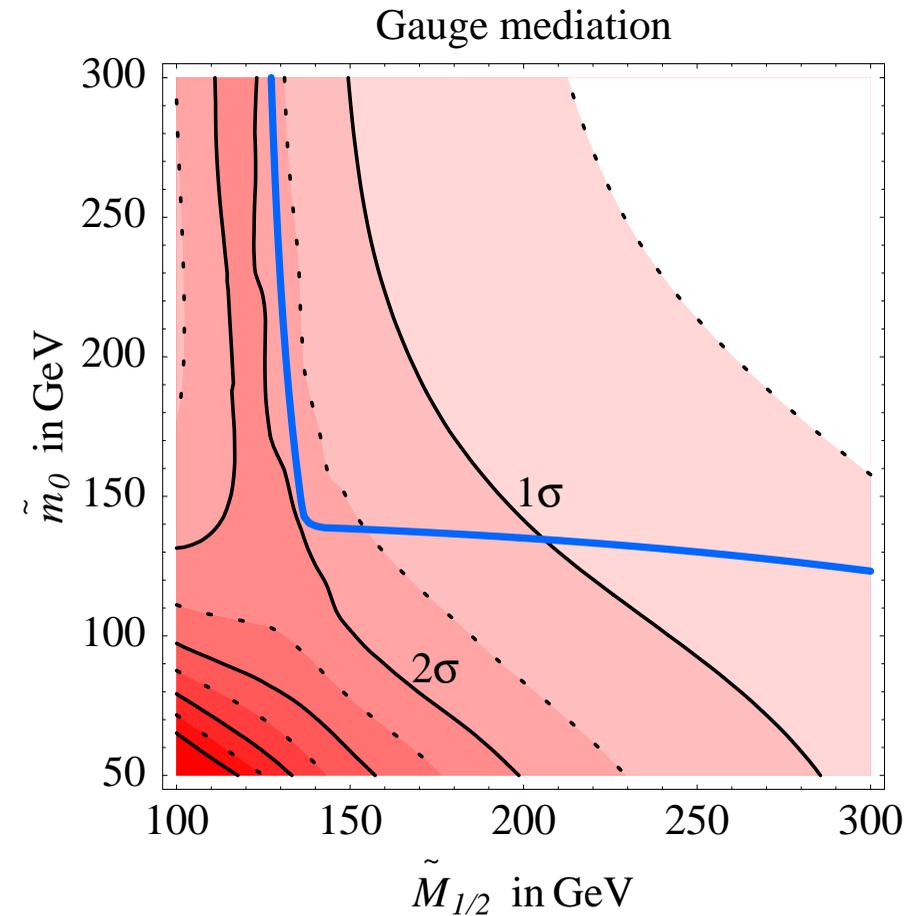
The thick blue line is the direct constraint $m_{\chi}, m_{\tilde{\ell}} > 100$ GeV

Gauge mediation

($\tan \beta = 10$, $M_{\text{GM}} = 10^{10}$ GeV, $\mu > 0$)



Without LEP2

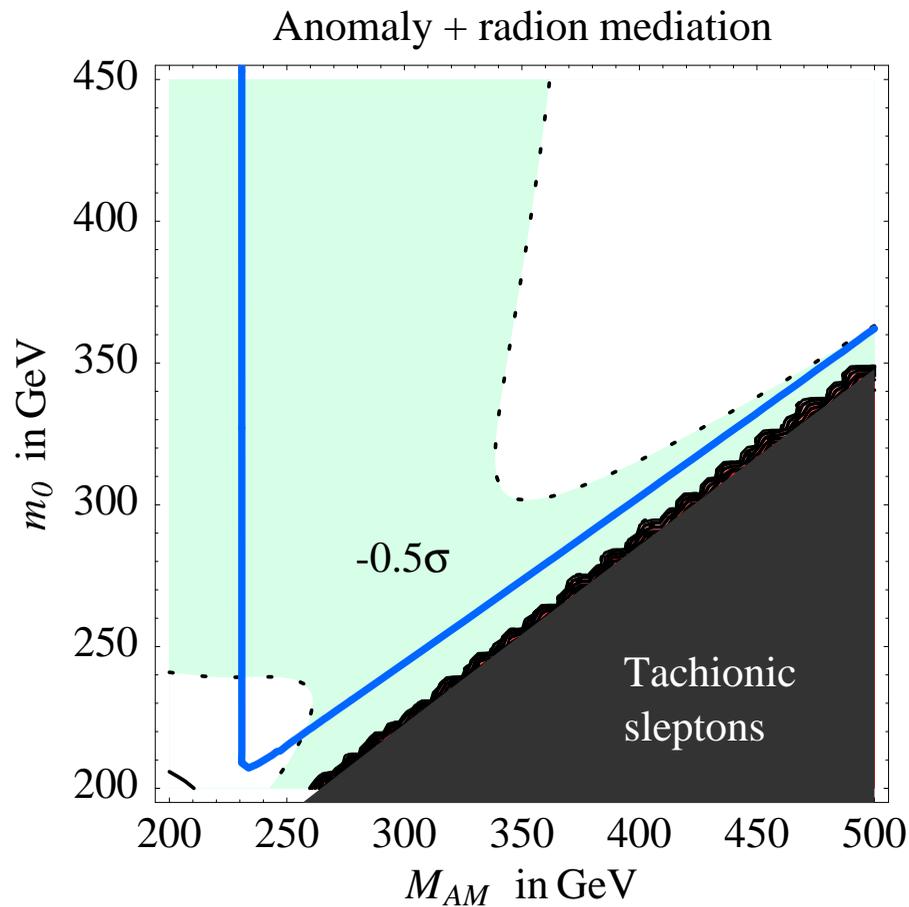


With LEP2

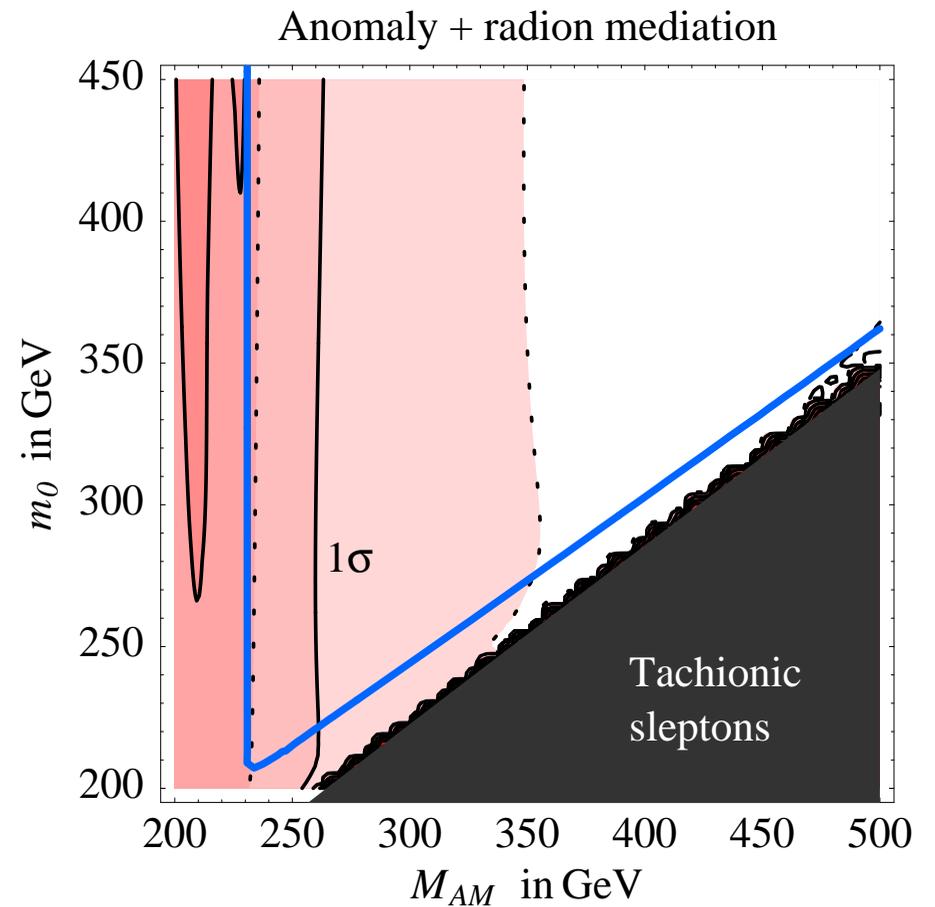
The thick blue line is the direct constraint $m_\chi, m_{\tilde{\ell}} > 100$ GeV

Anomaly + radion mediation

($\tan \beta = 10, \mu > 0$)



Without LEP2

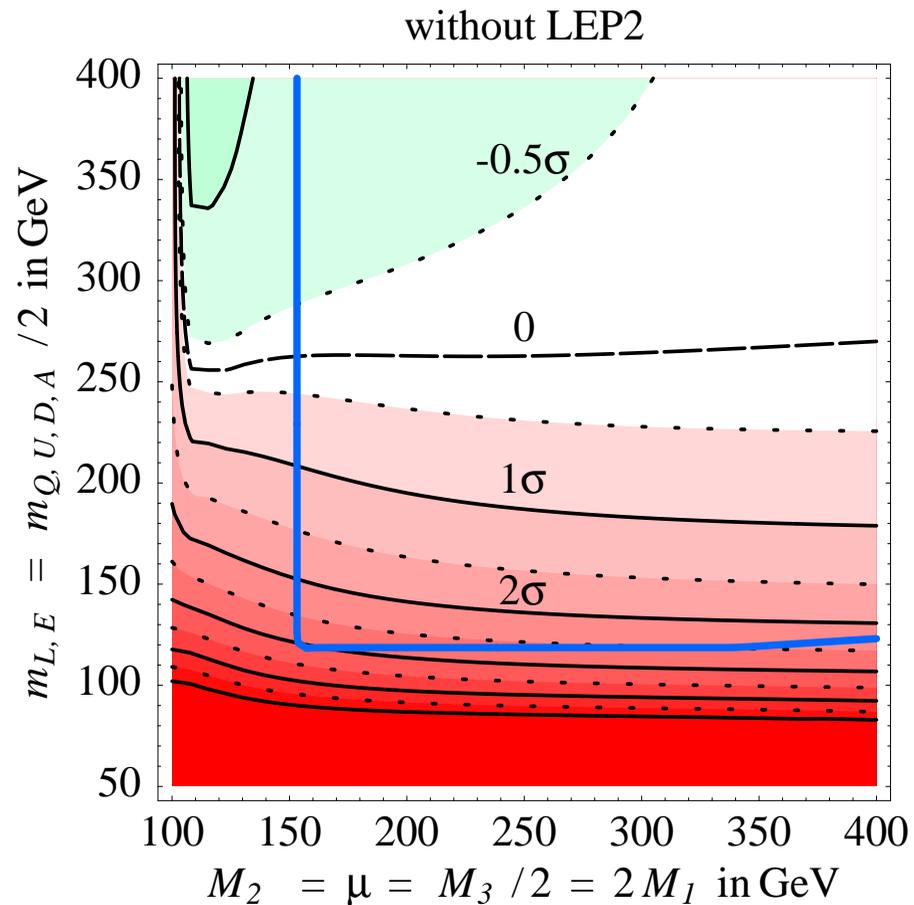


With LEP2

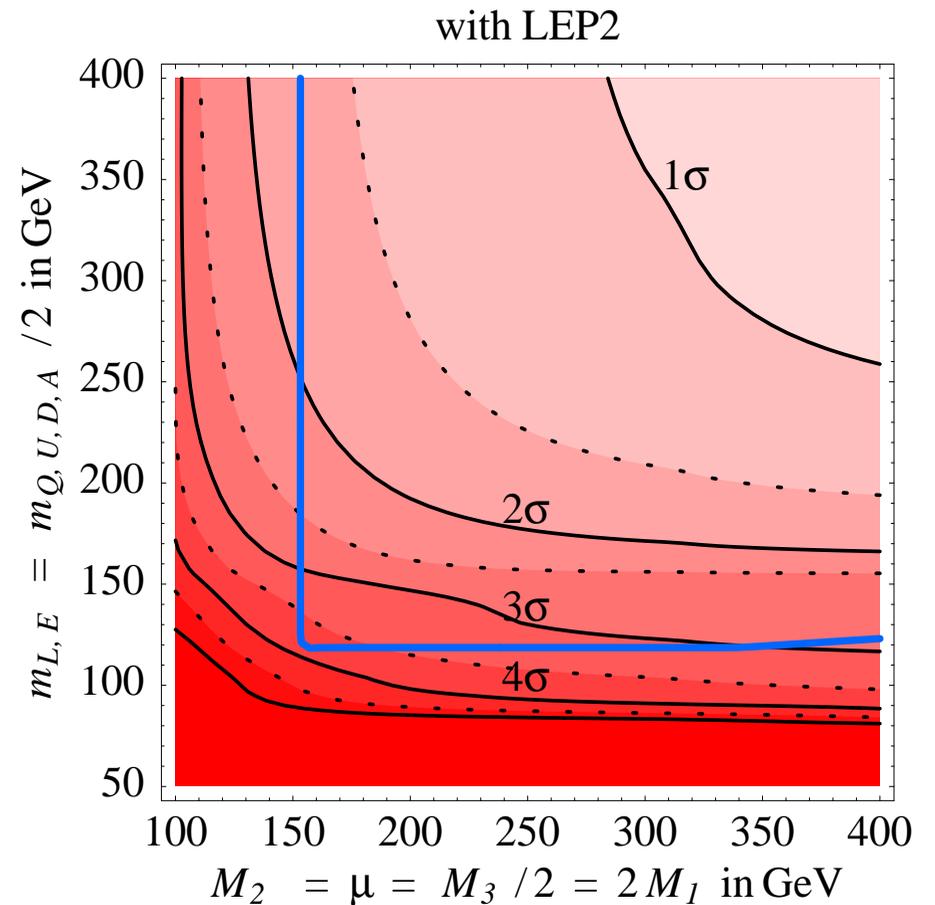
The thick blue line is the direct constraint $m_\chi, m_{\tilde{\ell}} > 100$ GeV

A simple model

chosen such that all sparticles can be at the same time as light as allowed by direct constraints (thick blue line)



Without LEP2



With LEP2

Conclusions

- Precision data: only constraints, but relevant for the hierarchy problem
- LEP2 $e\bar{e} \rightarrow f\bar{f}$ data are relevant
- Heavy universal models: \hat{S}, \hat{T}, W, Y (not S, T, U)
 - Gauge bosons in extra dimensions.
 - Higgsless.
 - Little Higgs: $f > \text{few TeV}$. $\hat{S} > (W + Y)/2$, $W, Y > 0$.
- Generic Z' approximated with leptonic \hat{S}, \hat{T}, W, Y
- Supersymmetry: LEP2 removes previous hints

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