

Impact of CP phases on the search for squarks \tilde{t} and \tilde{b}

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§1 Introduction

- So far most phenomenological studies on SUSY particle searches have been performed in the Minimal Supersymmetric Standard Model (MSSM) with real SUSY parameters.
- However it has recently been realized that the effects of the possible complex phases (or CP phases) of the SUSY parameters could be quite significant.
- The CP phases can significantly affect not only CP-violating observables (such as lepton EDMs) but also CP-conserving observables (such as decay branching ratios of the sparticles).
- Here we study the effect of the possible CP phases on the branching ratios of \tilde{t} and \tilde{b} decays.

• Purpose of this talk:

(i) Study $\tilde{t}_{1,2}$ and $\tilde{b}_{1,2}$ decays in the MSSM with complex SUSY parameters

(ii) Show that the effect of the CP phases of the complex parameters on the branching ratios of \tilde{t} and \tilde{b} decays can be quite strong in a significant portion of the MSSM parameter space.

(iii) Point out that this could have an important impact on the search for $\tilde{t}_{1,2}$ and $\tilde{b}_{1,2}$, and the determination of the MSSM parameters at future colliders such as LC and LHC.

§2 Basic parameters of MSSM with CP phases

* Basic parameters of MSSM:

$$\{ \tan\beta, M_2, \underline{M_1}, \underline{\mu}, \underline{A_{t,b}}, m_{\tilde{t}_1}, m_{\tilde{t}_2}, m_{\tilde{b}_1}, m_{H^+} \} \text{ (at } Q = m_Z \text{)}$$

* We take ($A_{t,b}$, μ , M_1) as complex parameters

| trilinear coupling: $\underline{A_{t,b}} = |A_{t,b}| e^{i\varphi_{A_{t,b}}} \quad (-\pi < \varphi_{A_{t,b}} < \pi)$

| higgsino mass parameter: $\underline{\mu} = |\mu| e^{i\varphi_\mu} \quad (-\pi < \varphi_\mu < \pi)$

| U(1) gaugino mass: $\underline{M_1} = |M_1| e^{i\varphi_1} \quad (-\pi < \varphi_1 < \pi)$

(note) The basic parameters determine all of the physics here.

(note) We do not assume the GUT relations among the soft-SUSY-breaking parameters such as $M_{\tilde{q}}$, $M_{\tilde{u}}$ and $M_{\tilde{d}}$, since the relations are highly model-dependent.

(note) In order to improve convergence of perturbative expansion, we use effective running quark masses

$$m_b^{\text{run}} = 3 \text{ GeV} \quad \& \quad m_t^{\text{run}} = 150 \text{ GeV}$$

for invariant amplitudes.

§3 CP phase dependence of masses, mixings, & couplings

(i) \tilde{t} masses & mixing;

- \tilde{t} mass matrix; $m_{\tilde{t}}^2 = \begin{pmatrix} m_{\tilde{t}_L}^2 & A_t^* m_t \\ A_t m_t & m_{\tilde{t}_R}^2 \end{pmatrix}$ (in $\tilde{t}_L - \tilde{t}_R$ base)

$$\begin{cases} m_{\tilde{t}_L}^2 = M_{\tilde{t}}^2 + (\text{D term})_L + m_t^2 \\ m_{\tilde{t}_R}^2 = M_{\tilde{t}}^2 + (\text{D term})_R + m_t^2 \\ A_t m_t = (A_t - \mu^* \cot\beta) m_t = |A_t m_t| e^{i\varphi_t} \end{cases}$$

- Diagonalizing the mass matrix we get mass eigenstates

\tilde{t}_1 and \tilde{t}_2 ;

$$\begin{pmatrix} \tilde{t}_1 \\ \tilde{t}_2 \end{pmatrix} = \begin{pmatrix} e^{i\varphi_t} \cos\theta_t & \sin\theta_t \\ -\sin\theta_t & e^{-i\varphi_t} \cos\theta_t \end{pmatrix} \begin{pmatrix} \tilde{t}_L \\ \tilde{t}_R \end{pmatrix}$$

Masses and mixing angle are given by

$$\begin{cases} m_{\tilde{t}_1}^2 = \frac{1}{2}(m_{\tilde{t}_L}^2 + m_{\tilde{t}_R}^2 + \sqrt{(m_{\tilde{t}_L}^2 - m_{\tilde{t}_R}^2)^2 + 4m_t^2 |A_t - \mu^* \cot\beta|^2}) \\ \tan 2\theta_t = \frac{2m_t |A_t - \mu^* \cot\beta|}{m_{\tilde{t}_L}^2 - m_{\tilde{t}_R}^2} \end{cases}$$

CP phase dependence;

- $m_{\tilde{t}_1}$ and θ_t are sensitive to the phases $(\varphi_{At}, \varphi_\mu)$
if $|A_t| \sim |\mu| \cot\beta$.

- \tilde{t} -mixing phase φ_t is sensitive
to the phases $\left\{ \frac{(\varphi_{At}, \varphi_\mu)}{\frac{\varphi_{At}}{\varphi_\mu}} \right\}$ if $\left\{ \begin{array}{l} |A_t| \sim |\mu| \cot\beta \\ \gg \\ \ll \end{array} \right\}$.

(ii) \tilde{b} masses & mixing;

- \tilde{b} mass matrix; $m_{\tilde{b}}^2 = \begin{pmatrix} m_{\tilde{b}_L}^2 & a_b^* m_b \\ a_b m_b & m_{\tilde{b}_R}^2 \end{pmatrix}$ (in $\tilde{b}_L - \tilde{b}_R$ -base)

$$\begin{cases} m_{\tilde{b}_L}^2 = M_Q^2 + (\text{D term})_L + m_b^2 \\ m_{\tilde{b}_R}^2 = M_D^2 + (\text{D term})_R + m_b^2 \\ a_b m_b = (A_b - \mu^* \tan \beta) m_b = |A_b m_b| e^{i \varphi_b} \end{cases}$$

- Diagonalizing the mass matrix we get mass eigenstates

\tilde{b}_1 and \tilde{b}_2 ;

$$\begin{pmatrix} \tilde{b}_1 \\ \tilde{b}_2 \end{pmatrix} = \begin{pmatrix} e^{i \varphi_b} \cos \theta_{\tilde{b}} & \sin \theta_{\tilde{b}} \\ -\sin \theta_{\tilde{b}} & e^{-i \varphi_b} \cos \theta_{\tilde{b}} \end{pmatrix} \begin{pmatrix} \tilde{b}_L \\ \tilde{b}_R \end{pmatrix}$$

Masses and mixing angle are given by

$$\begin{cases} m_{\tilde{b}_1} = \frac{1}{2} (m_{\tilde{b}_L}^2 + m_{\tilde{b}_R}^2 + \sqrt{(m_{\tilde{b}_L}^2 - m_{\tilde{b}_R}^2)^2 + 4 m_b^2 |A_b - \mu^* \tan \beta|^2}) \\ \tan 2\theta_{\tilde{b}} = \frac{2 m_b |A_b - \mu^* \tan \beta|}{m_{\tilde{b}_L}^2 - m_{\tilde{b}_R}^2} \end{cases}$$

CP phase dependence;

[— $m_{\tilde{b}_1}$ and $\theta_{\tilde{b}}$ are sensitive to the phases $(\varphi_{A_b}, \varphi_\mu)$
if $|A_b| \sim |\mu| \tan \beta$.

[— \tilde{b} -mixing phase $\varphi_{\tilde{b}}$ is sensitive
to the phases $\left\{ \frac{(\varphi_{A_b}, \varphi_\mu)}{\varphi_{A_b}} \right\}$ if $\left\{ \begin{array}{ll} |A_b| \sim |\mu| \tan \beta & \gg \\ & \ll \end{array} \right\}$.

(iii) $\tilde{\chi}^0$ & $\tilde{\chi}^\pm$ masses & mixings;

• $\tilde{\chi}^0$ mass matrix;

$$m_{\tilde{\chi}^0} = \begin{pmatrix} \tilde{B} & \tilde{W}^0 & \tilde{H}_1^0 & \tilde{H}_2^0 \\ M_1 & 0 & -m_Z \Delta \theta_W c\beta & m_Z \Delta \theta_W s\beta \\ 0 & M_2 & m_Z c\theta_W c\beta & -m_Z c\theta_W s\beta \\ -m_Z \Delta \theta_W c\beta & m_Z c\theta_W c\beta & 0 & -\mu \\ m_Z \Delta \theta_W s\beta & -m_Z c\theta_W s\beta & -\mu & 0 \end{pmatrix}$$

• $\tilde{\chi}^\pm$ mass matrix;

$$m_{\tilde{\chi}^\pm} = \begin{pmatrix} M_2 & \sqrt{2} m_W s\beta \\ \sqrt{2} m_W c\beta & \mu \end{pmatrix}$$

• CP phase dependence;

- $m_{\tilde{\chi}_1^0}$ and $\tilde{\chi}^0$ -mixing matrix are sensitive to (g_μ, g_i)
for small $\tan\beta$.
- $m_{\tilde{\chi}_1^\pm}$ and $\tilde{\chi}^\pm$ -mixing matrices are sensitive to g_μ
for small $\tan\beta$.

(iv) H_i^0 masses & mixing;

• H_i^0 mass matrix;

H_i^0 mass matrix of the Higgs sector with explicit CP violation is given by

$$m_{H^0}^2 = \begin{pmatrix} \Phi_1 & \Phi_2 & a \\ \Phi_1 & m_1^2 & m_{12}^2 & m_{1a}^2 \\ \Phi_2 & m_{12}^2 & m_2^2 & m_{2a}^2 \\ a & m_{1a}^2 & m_{2a}^2 & m_a^2 \end{pmatrix} \quad (\text{Carena et al., N.P.B586(2000)92})$$

(CP even)-(CP odd) mixing terms m_{1a}^2 :

$$\underline{m_{1a}^2 \propto \text{Im}(A_{t,b}\mu)} \sim |A_{t,b}| |\mu| \sin(\underline{\vartheta_{At,b} + \vartheta_\mu}).$$

• CP phase dependence;

- Mass eigenvalues $m_{H_i^0}$ ($i=1,2,3$) are sensitive to phase sum $(\vartheta_{At,b} + \vartheta_\mu)$ for small $\tan\beta$. ($m_{H_1^0} < m_{H_2^0} < m_{H_3^0}$)
- H_i^0 -mixing matrix (O_{ij}) is sensitive to $(\vartheta_{At,b} + \vartheta_\mu)$ for any $\tan\beta$. $\left(\begin{pmatrix} H_1^0 \\ H_2^0 \\ H_3^0 \end{pmatrix} = \begin{pmatrix} O^\top \end{pmatrix} \begin{pmatrix} \Phi_1 \\ \Phi_2 \\ a \end{pmatrix} \right)$

(v) Couplings among interaction-eigenstates;

Squark-chirality flip couplings to Higgs bosons
depend on the phases ($\phi_{A_{t,b}}, \phi_\mu$):

$$C(\tilde{b}_L^\dagger \tilde{t}_R H^-) \sim \sin\beta h_t (A_t^* \cot\beta + \mu)$$

$$C(\tilde{t}_L^\dagger \tilde{b}_R H^+) \sim \cos\beta h_b (A_b^* \tan\beta + \mu)$$

$$C(\tilde{b}_L^\dagger \tilde{b}_R \phi_1) \sim h_b A_b^*$$

$$C(\tilde{b}_L^\dagger \tilde{b}_R \phi_2) \sim h_b \mu$$

$$C(\tilde{b}_L^\dagger \tilde{b}_R a) \sim \cos\beta h_b (A_b^* \tan\beta + \mu)$$

$$C(\tilde{t}_L^\dagger \tilde{t}_R a) \sim \sin\beta h_t (A_t^* \cot\beta + \mu)$$

(vi) Decay widths (and hence branching ratios) and
cross sections are functions of the masses, mixings and
couplings of the involved particles.

(ex) The production cross sections of

$$e^+ e^- \rightarrow \tilde{t}_i \bar{\tilde{t}}_j \quad \& \quad \tilde{b}_i \bar{\tilde{b}}_j$$

are functions of the masses and mixing angles of
 \tilde{t}_i and \tilde{b}_i .

(vii) CP phase dependence of the production cross sections
and the decay branching ratios of $\tilde{t}_{1,2}$ & $\tilde{b}_{1,2}$;

From these observations (i)~(vi), we expect that
the production cross sections and the decay branching
ratios of $\tilde{t}_{1,2}$ and $\tilde{b}_{1,2}$ can be sensitive to the CP phases
($\vartheta_{A_{t,b}}, \vartheta_\mu, \vartheta_i$)!

§4 Impact of CP phases on $\tilde{t}_{1,2}$ & $\tilde{b}_{1,2}$ decays

(i) $\tilde{t}_{1,2}$ & $\tilde{b}_{1,2}$ decays;

Possible important decays are

- | $\tilde{t}_1 \rightarrow t \tilde{g}, t \tilde{\chi}_1^0, b \tilde{\chi}_2^+, \tilde{b}_1 W^+, \tilde{b}_1 H^+$
- | $\tilde{t}_2 \rightarrow t \tilde{g}, t \tilde{\chi}_1^0, b \tilde{\chi}_2^+, \tilde{t}_1 \tilde{\chi}_1^0, \tilde{b}_2 W^+, \tilde{t}_1 H_1^0, \tilde{b}_2 H^+$
- | $\tilde{b}_1 \rightarrow b \tilde{g}, b \tilde{\chi}_1^0, t \tilde{\chi}_2^-, \tilde{t}_1 W^-, \tilde{t}_1 H^-$
- | $\tilde{b}_2 \rightarrow b \tilde{g}, b \tilde{\chi}_1^0, t \tilde{\chi}_2^-, \tilde{b}_1 \tilde{\chi}_1^0, \tilde{t}_2 W^-, \tilde{b}_1 H_1^0, \tilde{t}_2 H^-$

(ii) Constraints on MSSM;

In the plots we impose the following conditions in order to respect experimental and theoretical constraints:

- $m_{\tilde{\chi}_1^+} > 103 \text{ GeV}, m_{\tilde{\chi}_1^0} > 50 \text{ GeV}, m_{H_1^0} > 105 \text{ GeV},$
 $m_{\tilde{t}_1, \tilde{b}_1} > 100 \text{ GeV}, m_{\tilde{t}_1, \tilde{b}_1} > m_{\tilde{\chi}_1^0} \quad (\text{LEP limits})$
- $|A_t|^2 < 3(M_{\tilde{Q}}^2 + M_{\tilde{U}}^2 + m_{H_2}^2)$
 $|A_b|^2 < 3(M_{\tilde{Q}}^2 + M_{\tilde{D}}^2 + m_{H_1}^2)$
(vacuum stability condition)
- $\Delta \rho(\tilde{t} - \tilde{b}) < 0.0012$
(limit from the precision data on the $\tilde{t} - \tilde{b}$ loop contribution to ρ parameter)
- $2.0 \times 10^{-4} < B(b \rightarrow s \gamma) < 4.5 \times 10^{-4}$ (BELLE, CLEO)
(assuming the CKM mixing also for the \tilde{q} sector)

(Note 1) electron & neutron EDM constraints on MSSM;

- *In general the experimental limits on e & n EDMs strongly constrain the SUSY CP phases.*
- *One interesting possibility for evading these constraints is to invoke large masses (much above the TeV scale) for the 1st two generations of the sfermions , keeping the 3rd generation sfermions relatively light ($\lesssim 1$ TeV).*
- *In such a scenario the CP phases ($g_1, g_\mu, g_{A\tau}, g_{A\pm}, g_{A\delta}$) are practically unconstrained. We take this scenario.*

*See Cohen-Kaplan-Nelson, Phys. Lett. B388 (1996) 588;
Carena-Ellis-Pilaftsis-Wagner, Nucl.Phys.B586(2000)92;
Akeroyd-Keum-Recksiegel, Phys. Lett. B 507 (2001) 252.*

(iii) Results on \tilde{t}_1 decays;

- $(\mathcal{S}_{At}, \mathcal{S}_\mu)$ dependence;

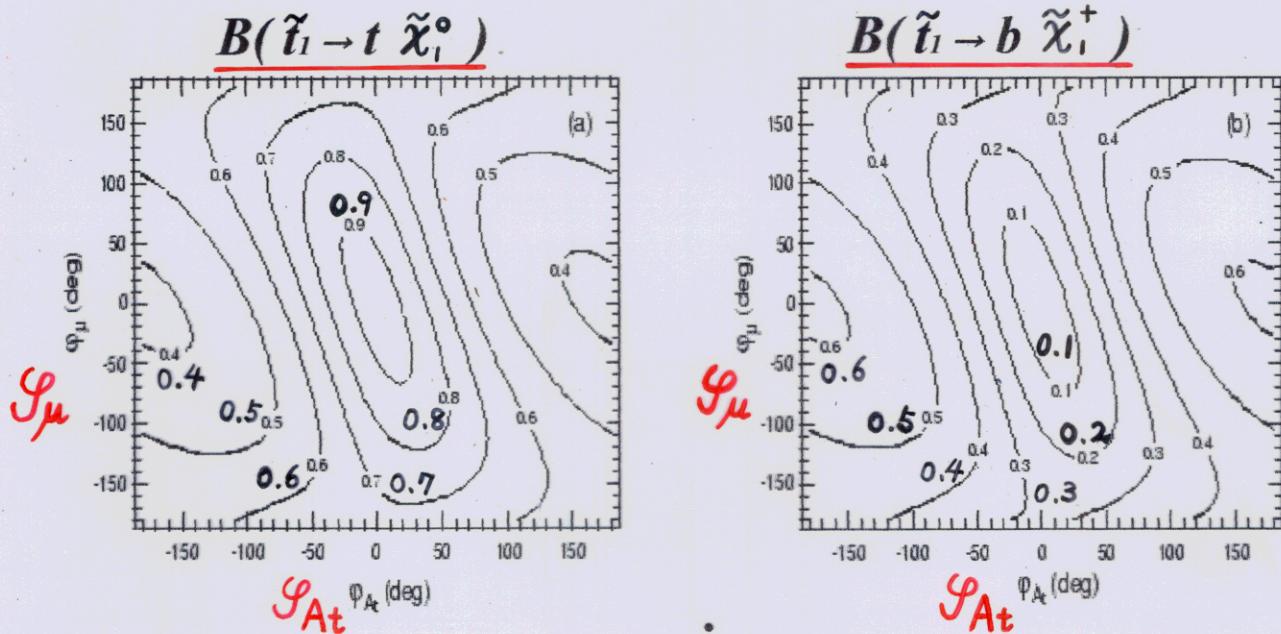


Figure 2: Contours of the \tilde{t}_1 decay branching ratios $B(\tilde{t}_1 \rightarrow t \tilde{\chi}_1^0)$ (a) and $B(\tilde{t}_1 \rightarrow b \tilde{\chi}_1^+)$ (b) in the φ_{At} - φ_μ plane for $\tan \beta = 8$, $(m_{\tilde{t}_1}, m_{\tilde{t}_2}, m_{\tilde{\chi}_1}) = (400, 700, 200)$ GeV, $|A| = 800$ GeV, $|\mu| = 500$ GeV, $\varphi_{At} = \varphi_1 = 0$, and $m_{H^\pm} = 600$ GeV in the case $m_{\tilde{t}_L} \geq m_{\tilde{t}_R}$.

$$|At| = |Ab| = |A|, \quad M_2 = 300 \text{ GeV}$$



(The \tilde{t}_1 decay branching ratios can depend on the phases)
 ($\mathcal{S}_{At}, \mathcal{S}_\mu$) quite strongly!

(iv) Results on \tilde{b}_1 decays;

-- φ_{Ab} dependence;

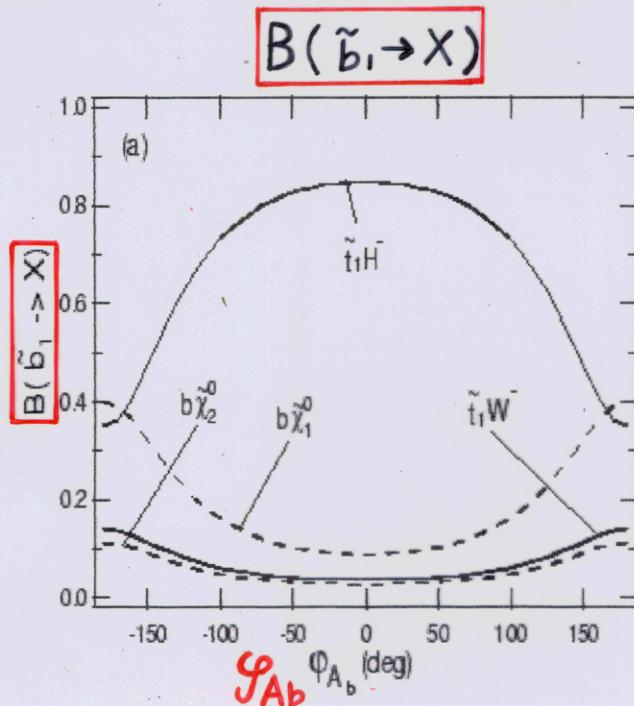


Figure 5: φ_{Ab} dependence of the \tilde{b}_1 (a) [\tilde{b}_2 (b)] decay branching ratios for $\tan \beta=30$, $(m_{\tilde{t}_1}, m_{\tilde{t}_2}, m_{\tilde{b}_1}) = (200, 700, 400)$ GeV [(175, 500, 350) GeV], $(|A|, |\mu|) = (800, 700)$ GeV [(600, 500) GeV], $\varphi_{A_t} = \varphi_\mu = \pi$, $\varphi_1 = 0$, and $m_{H^\pm} = 180$ GeV in the case $m_{\tilde{t}_L} \geq m_{\tilde{t}_R}$.

$$|A_t| = |A_b| = |A|, M_2 = 300 \text{ GeV}$$



(The \tilde{b}_1 decay branching ratios can be very sensitive to)
the phase φ_{Ab} !)

(v) Results on \tilde{t}_2 decays;

-- φ_{At} dependence;

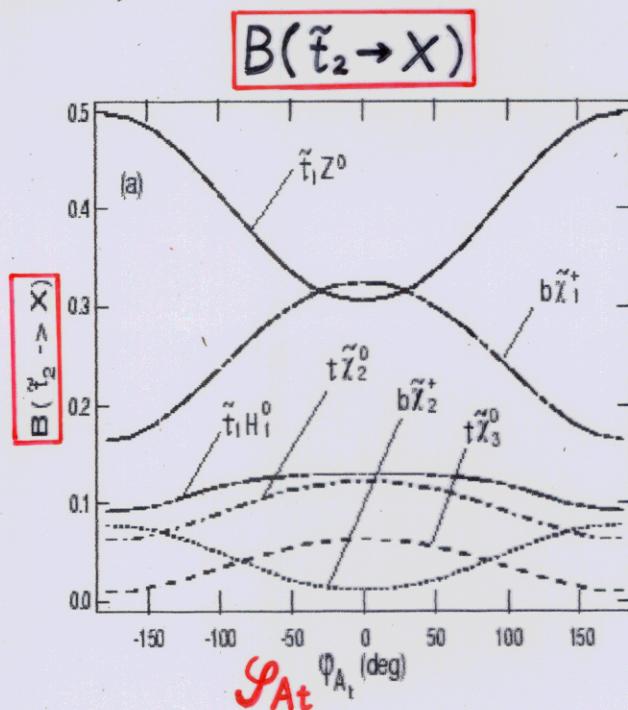


Figure 4: φ_{At} dependence of the \tilde{t}_2 decay branching ratios for $\varphi_\mu = 0$ (a) and $\pi/2$ (b) with $\tan \beta = 8$, $(m_{\tilde{t}_1}, m_{\tilde{t}_2}, m_{\tilde{b}_1}) = (400, 700, 200)$ GeV, $|A| = 800$ GeV, $|\mu| = 500$ GeV, $\varphi_{A_b} = \varphi_1 = 0$, and $m_{H^\pm} = 600$ GeV in the case $m_{\tilde{t}_L} \geq m_{\tilde{t}_R}$. Note that the $\tilde{t}_1 H_{2,3}^0$ and $\tilde{b}_1 H^\pm$ modes are kinematically forbidden here.

$$|At| = |Ab| = |A|, M_2 = 300 \text{ GeV}$$



**(The \tilde{t}_2 decay branching ratios can be very sensitive
to the phase φ_{At} !)**

(V) Results on \tilde{b}_2 decays;

- φ_{Ab} dependence;

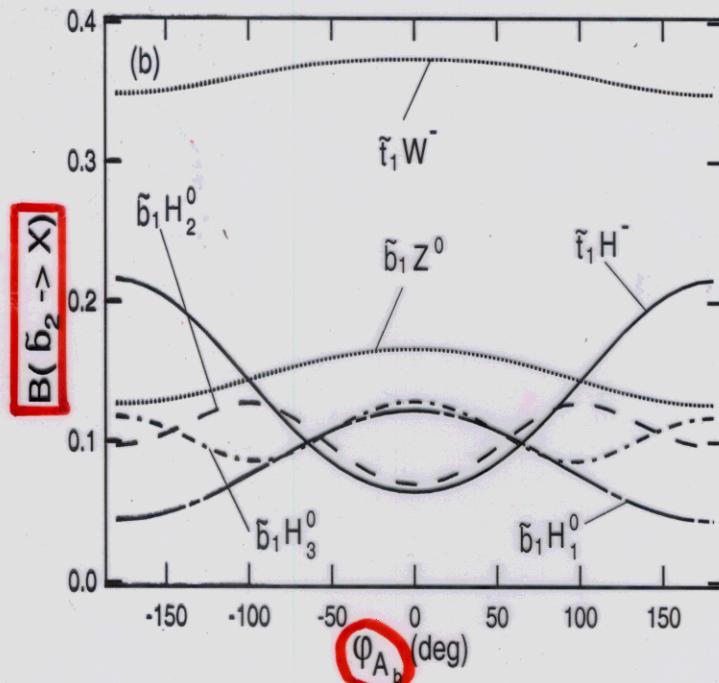


Figure 5: φ_{Ab} dependence of the \tilde{b}_1 (a) [\tilde{b}_2 (b)] decay branching ratios for $\tan\beta=30$, $(m_{\tilde{t}_1}, m_{\tilde{t}_2}, m_{\tilde{b}_1}) = (200, 700, 400)$ GeV [(175, 500, 350) GeV], $(|A|, |\mu|) = (800, 700)$ GeV [(600, 500) GeV], $\varphi_{At} = \varphi_\mu = \pi$, $\varphi_1 = 0$, and $m_{H^\pm} = 180$ GeV in the case $m_{\tilde{t}_L} \geq m_{\tilde{t}_R}$. Only interesting modes are shown in Fig.b where we have $m_{\tilde{b}_2} \sim 570$ GeV and $(m_{H_1^0}, m_{H_2^0}, m_{H_3^0}) \sim (114, 156, 158)$ GeV.

$$|At| = |Ab| = |A|, M2 = 300 \text{ GeV}$$



The \tilde{b}_2 decay branching ratios can be very sensitive
to the phase φ_{Ab} !

(vi) Impact of CP phases;

- The CP phases can significantly affect not only CP-violating observables (such as the lepton EDM) but also CP-conserving quantities (such as the branching ratios of the $\tilde{t}_{1,2}$ and $\tilde{b}_{1,2}$ decays).
- Hence the possible sizable phases could have important consequences for the determination of the basic MSSM-parameters from measurements of the observables, since almost none of the basic MSSM-parameters are directly measured.

5 Impact of CP phases on the MSSM parameter determination

-- Observables (such as masses, cross sections & branching ratios) are functions of the basic MSSM-Parameters.

$$\begin{cases} O_1 = O_1(P_1, \dots, P_n) \\ \vdots \\ O_N = O_N(P_1, \dots, P_n) \end{cases} \quad (\underline{N > n})$$

$\{O_1, \dots, O_N\} = \{\text{masses, cross sections, branching ratios}\}$

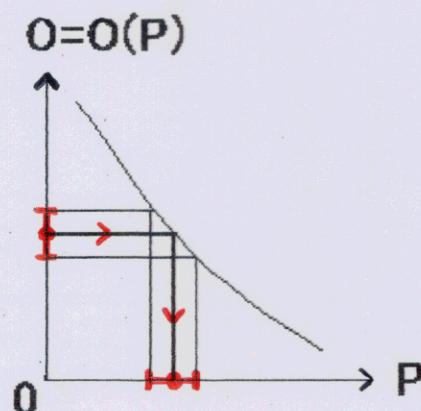
$\{P_1, \dots, P_n\} = \{\tan\beta, M_2, M_1, \mu, A_{t,b}, \dots\}$

-- These observables $\{O_1, \dots, O_N\}$ over-constrain the basic MSSM-parameters $\{P_1, \dots, P_n\}$!

-- So, we can determine these parameters $\{P_j\}$ and their errors $\{\Delta P_j\}$ by a χ^2 -fit to the experimental data of these observables $\{O_i \pm \Delta O_i\}$.

$$\underline{O_i = O_i(P_j)} \quad (\{O_i\} \text{ over-constrain } \{P_j\})$$

$$\underline{\{O_i \pm \Delta O_i\} \rightarrow \{P_j \pm \Delta P_j\} \quad (\text{by a } \chi^2\text{-fit})}$$



-- If these parameters $\{P_j\}$ are actually complex, then real parameter fit would result in a totally wrong MSSM parameter determination !

● Example of Impact - a case study;

(i) Assumptions;

We assume the following situation:

(1) At LHC;

$m_{\tilde{g}}$ can be measured with 3% error.

(pri. com. with A. De Roeck)

(2) At TESLA (GLC) ($\sqrt{s} < 1 \text{ TeV}$);

- $m_{\tilde{\chi}_i^+}, m_{\tilde{\chi}_i^0}, m_{H_i^0}$ can be measured with high accuracy.
(e.g. $\Delta m_{\tilde{\chi}_i^+} = 0.2 \text{ GeV}$, $\Delta m_{\tilde{\chi}_i^0} = 0.3 \text{ GeV}$, $\Delta m_{H_i^0} = 0.05 \text{ GeV}$)
- $m_{H_2^0}, m_{H_3^0}, m_{H^+}$ ($\lesssim 500 \text{ GeV}$) can with error of 1.5 GeV.
- $m_{\tilde{t}_{1,2}}, m_{\tilde{b}_{1,2}}$ ($\lesssim 500 \text{ GeV}$) can with 1% error.

$\begin{cases} \text{TESLA (TDR), hep-ph/0106315;} \\ \text{E. Accomando et al., Phys.Rep.229(1998)1;} \\ \text{H.Martyn, G.Blair, hep-ph/9910416} \end{cases}$

(3) At CLIC ($\sqrt{s} = 2 \text{ TeV}$ e^+e^- Collider);

- $m_{H_2^0}$, $m_{H_3^0}$, m_{H^+} ($>500\text{GeV}$) can be measured with 1% error.

- $m_{\tilde{t}_{1,2}}$, $m_{\tilde{b}_{1,2}}$ ($>500\text{GeV}$) can ... with 3% error.

(pri. com. with A. De Roeck & M. Battaglia)

- We can get e^- & e^+ beam helicity-polarizations of $P(e^-) = 80\%$ & $P(e^+) = 40\%$.

(Note) We do not take into account additional information from LHC on \tilde{t} and \tilde{b} systems because the amount of information available strongly depends on the scenario realized in nature.

(pri. com. with G. Polesello)

(ii) Strategy:

Our strategy is as follows:

(Step 1) Take a specific set of values of the basic MSSM-parameters:

$$\{ \tan\beta, M_{\tilde{Q}}, M_{\tilde{U}}, M_{\tilde{D}}, |A_t|, |A_b|, \varphi_{A_t}, \varphi_{A_b}, \varphi_i, M_2, |\mu|, \varphi_\mu, m_{\tilde{\chi}^0}, m_{H^+} \}$$

(Step 2) Calculate the observables:

- masses of $\tilde{t}_i, \tilde{b}_i, \tilde{\chi}_j^0, \tilde{\chi}_k^+, H^\circ$
- production cross sections of $e_\uparrow^+ e_\uparrow^- \rightarrow \tilde{t}_i \bar{\tilde{t}}_j \text{ & } \tilde{b}_i \bar{\tilde{b}}_j$
- branching ratios of \tilde{t}_i & \tilde{b}_i decays

(Step 3) Regard these calculated values of the observables as real "experimental data" with definite errors.

(Note) For the cross sections & branching ratios, we take only statistical errors for $L=1ab^{-1}$ at $\sqrt{s}=2TeV$ (at CLIC). We have doubled these statistical errors for safety.

(Step 4) Determine the basic MSSM-parameters and their errors by a χ^2 -fit to the "experimental data".

(iii) Scenarios; (STEP 1)

We consider 2 typical scenarios:

- Small $\tan\beta$ (=6) scenario;

The basic MSSM-parameters:

$$\tan\beta = 6,$$

$$(M_{\tilde{Q}}, M_{\tilde{U}}, M_{\tilde{D}}) = (623, 409, 107) \text{ GeV},$$

$$|A_t| = |A_b| = 800 \text{ GeV},$$

$$\varphi_{At} = \varphi_{Ab} = \pi/4, \varphi_i = 0,$$

$$M_2 = 300 \text{ GeV}, \mu = -350 \text{ GeV},$$

$$m_{\tilde{g}} = 1000 \text{ GeV}, m_{H^\pm} = 900 \text{ GeV}$$

- Large $\tan\beta$ (=30) scenario;

The basic MSSM-parameters:

$$\tan\beta = 30,$$

$$(M_{\tilde{Q}}, M_{\tilde{U}}, M_{\tilde{D}}) = (692, 198, 360) \text{ GeV},$$

$$|A_t| = 600 \text{ GeV}, |A_b| = 1000 \text{ GeV},$$

$$\varphi_{At} = \pi/4, \varphi_{Ab} = 3\pi/2, \varphi_i = 0,$$

$$M_2 = 200 \text{ GeV}, \mu = -350 \text{ GeV},$$

$$m_{\tilde{g}} = 1000 \text{ GeV}, m_{H^\pm} = 350 \text{ GeV}$$

(→ For the calculated branching ratios, see Table.1.)

(STEP 2) & (STEP 3)

Calculated Masses with assumed errors :

- Small $\tan\beta$ ($=6$) scenario;

$$m \tilde{t}_1 = (350 \pm 3.5) \text{ GeV}, \quad m \tilde{t}_2 = (700 \pm 21) \text{ GeV},$$

$$m \tilde{b}_1 = (170 \pm 1.7) \text{ GeV}, \quad m \tilde{b}_2 = (626 \pm 19) \text{ GeV},$$

...

- Large $\tan\beta$ ($=30$) scenario;

$$m \tilde{t}_1 = (210 \pm 2.1) \text{ GeV}, \quad m \tilde{t}_2 = (729 \pm 22) \text{ GeV},$$

$$m \tilde{b}_1 = (350 \pm 3.5) \text{ GeV}, \quad m \tilde{b}_2 = (700 \pm 21) \text{ GeV},$$

...

Calculated cross sections of $e^- e^+ \rightarrow \tilde{t}_i \bar{\tilde{t}}_i$ & $\tilde{b}_i \bar{\tilde{b}}_i$:

$\tan(\beta) = 6$ scenario

Cross sections (ab): (at $\sqrt{s} = 2$ TeV (CLIC))

$(P(e^-), P(e^+))$	(0.8, -0.4)	(-0.8, 0.4)
(stop_1 stop_1)	6003	11861
(stop_1 stop_2)	987	738
(stop_2 stop_1)	987	738
(stop_2 stop_2)	11263	1390
(sbot_1 sbot_1)	1290	4378
(sbot_1 sbot_2)	5	4
(sbot_2 sbot_1)	5	4
(sbot_2 sbot_2)	11009	1063

$\tan(\beta) = 30$ scenario

Cross sections (ab): (at $\sqrt{s} = 2$ TeV (CLIC))

$(P(e^-), P(e^+))$	(0.8, -0.4)	(-0.8, 0.4)
(stop_1 stop_1)	1151	16177
(stop_1 stop_2)	334	249
(stop_2 stop_1)	334	249
(stop_2 stop_2)	10570	950
(sbot_1 sbot_1)	1152	3678
(sbot_1 sbot_2)	67	50
(sbot_2 sbot_1)	67	50
(sbot_2 sbot_2)	8352	793

$\left(\text{with doubled statistical errors for } L = 1 \text{ ab}^{-1} \right)$
 at $\sqrt{s} = 2$ TeV (at CLIC)

(Table.1) Calculated branching ratios:

Table 1: Decay branching ratios (in %) for top squarks and bottom squarks in the two considered scenarios. Corresponding values of the underlying MSSM parameters are given in the text.

channel	scenario with $\tan \beta = 6$				scenario with $\tan \beta = 30$			
	\tilde{t}_1	\tilde{t}_2	\tilde{b}_1	\tilde{b}_2	\tilde{t}_1	\tilde{t}_2	\tilde{b}_1	\tilde{b}_2
$q\tilde{\chi}_1^0$	66.4	1.6	100	0.6	0	0.6	63.5	0.6
$q\tilde{\chi}_2^0$	0	7.5	0	8.7	0	8.5	36.1	10.3
$q\tilde{\chi}_3^0$	0	13.1	0	0.3	0	11.1	0	4.6
$q\tilde{\chi}_4^0$	0	6.6	0	2.4	0	8.7	0	4.6
$q'\tilde{\chi}_1^\pm$	33.1	19.2	0	9.7	100	22.5	0	14.1
$q'\tilde{\chi}_2^\pm$	0	1.6	0	21.0	0	6.8	0	24.2
$W^\pm \tilde{q}_1$	0.5	0.3	0	56.8	0	3.1	0.4	27.1
$H^\pm \tilde{q}_1$	0	0	0	0	0	7.7	0	6.4
$Z\tilde{q}_1$	—	26.9	—	0.2	—	13.1	—	1.5
$H_1\tilde{q}_1$	—	23.4	—	0.2	—	12.7	—	1.4
$H_2\tilde{q}_1$	—	0	—	0	—	2.8	—	2.7
$H_3\tilde{q}_1$	—	0	—	0	—	2.4	—	2.7

(with doubled statistical errors
 for $L = 1 \text{ ab}^{-1}$ at $\sqrt{s} = 2 \text{ TeV}$ (at CLIC))

(iv) Results of χ^2 -fit ; (STEP 4)

We determine the basic MSSM-parameters and their errors by a χ^2 -fit to the "experimental data" of the observables:

(Results of χ^2 -fit)

Table 2: Extracted parameters from the "experimental data" of the masses, production cross sections and decay branching ratios of \tilde{t}_i and \tilde{b}_i . The original parameters for each scenario are given in the text.

scenario	<u>$\tan \beta = 6$ scenario</u>	<u>$\tan \beta = 30$ scenario</u>
M_D^2	$(2.88 \pm 0.06) \times 10^4$	$(1.30 \pm 0.02) \times 10^5$
M_U^2	$(1.67 \pm 0.04) \times 10^5$	$(3.93 \pm 0.12) \times 10^4$
M_Q^2	$(3.88 \pm 0.04) \times 10^5$	$(4.79 \pm 0.04) \times 10^5$
$\text{Re}(A_t)$	<u>565.0 ± 13.0</u>	<u>424.0 ± 14.0</u>
$\text{Im}(A_t)$	<u>$\pm 566.0 \pm 14.0$</u>	<u>$\pm 425.0 \pm 15.0$</u>
$\text{Re}(A_b)$	<u>620.0 ± 190.0</u>	<u>6.5 ± 420.0</u>
$\text{Im}(A_b)$	<u>$\pm 230.0 \pm 580.0$</u>	<u>$\pm 999.0 \pm 52.0$</u>
$\text{Re}(M_1)$	149.3 ± 0.3	99.6 ± 0.6
$\text{Im}(M_1)$	1.0 ± 1.5	-0.5 ± 2.8
M_2	300.0 ± 0.4	200.0 ± 0.5
$\text{Re}(\mu)$	-350.0 ± 0.3	-350.0 ± 0.6
$\text{Im}(\mu)$	-0.02 ± 0.9	1.5 ± 5.0
$\tan \beta$	<u>6.0 ± 0.2</u>	<u>30.0 ± 0.8</u>
$m_{\tilde{g}}$	1000.0 ± 30	1000.0 ± 30
m_{H^\pm}	900.0 ± 5.0	350.0 ± 0.8

(Note) The sign ambiguity for Im parts of the parameters is due to the fact that we consider CP-even observables. This ambiguity can be resolved by considering appropriate CP-odd observables in the analysis.

See Aoki-Oshima, Mod.Phys.Lett. A13(1998)3225;

Yang-Du, P.R.D65(2002)115005;

Bartl et al., hep-ph/0202198 & hep-ph/0306304



All parameters except A_b can be determined rather precisely:

$\tan\beta$	with 3% error
$M_{\tilde{q}}, M_{\tilde{U}}, M_{\tilde{D}}$	with 1% to 2% errors
A_t	with 2% to 3% error
A_b	with 50% error

(Note) The reason why the error of A_b is so large:

Sbottom masses and mixing angle are rather insensitive to A_b due to small m_b (=5GeV).

*So, the observables are rather insensitive to A_b .
This leads to the large error of A_b .*

(Note) Real parameter fit;

The χ^2 -fit by using only real parameters results in a much larger χ^2 value ! :

$$\Delta\chi^2 \equiv \chi^2(\text{real para. fit}) - \chi^2(\text{complex para. fit})$$

<u>$\Delta\chi^2 = 287$</u> , $DOF = 61$	<u>(for $\tan\beta = 6$ scenario)</u>
<u>$\Delta\chi^2 = 23$</u> , $DOF = 61$	<u>(for $\tan\beta = 30$ scenario)</u>

(Result of Real Parameter Fit)

scenario	<u>$\tan \beta = 6$</u> scenario	<u>$\tan \beta = 30$</u> scenario
M_D^2	$(2.879 \pm 0.059) \times 10^4$	$(1.311 \pm 0.021) \times 10^5$
M_U^2	$(1.501 \pm 0.028) \times 10^5$	$(3.938 \pm 0.12) \times 10^4$
M_Q^2	$(4.022 \pm 0.041) \times 10^5$	$(4.802 \pm 0.038) \times 10^5$
$\text{Re}(A_t)$	<u>606.3 ± 8.6</u>	<u>600.4 ± 9.0</u>
$\text{Im}(A_t)$	<u>0</u>	<u>0</u>
$\text{Re}(A_b)$	<u>644.4 ± 210</u>	<u>1016 ± 58</u>
$\text{Im}(A_b)$	<u>0</u>	<u>0</u>
$\text{Re}(M_1)$	149.6 ± 0.31	99.55 ± 0.62
$\text{Im}(M_1)$	0	0
M_2	301.1 ± 0.38	199.9 ± 0.47
$\text{Re}(\mu)$	-349.5 ± 0.25	-350.0 ± 0.64
$\text{Im}(\mu)$	0	0
$\tan \beta$	<u>6.399 ± 0.14</u>	29.20 ± 0.63
$m_{\tilde{g}}$	1000.0 ± 30	1000.0 ± 30
m_{H^+}	900.0 ± 5.2	351.0 ± 0.85
χ^2	286.6	22.5



(Real parameter fit results in a totally
 wrong MSSM parameter determination!)

6 Conclusion

- We have shown that the effect of the CP phases of the complex parameters $A_{t,b}$, μ and M_1 on the branching ratios of the $\tilde{t}_{1,2}$ and $\tilde{b}_{1,2}$ decays can be quite strong in a significant portion of the MSSM parameter space.
- This could have an important impact on
 - (i) the search for $\tilde{t}_{1,2}$ and $\tilde{b}_{1,2}$,
and
 - (ii) the determination of the basic MSSM-parameters
at future colliders such as LC & LHC.